

# Introduction to Applied Scientific Computing using MATLAB

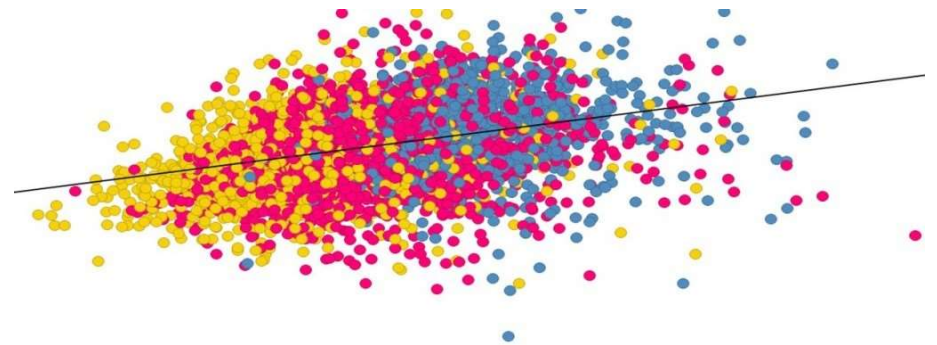
Mohsen Jenadeleh

**In this lecture, slides from MIT, Rutgers and Waterloo University are used to form the lecture slides**

## Connect Activity

Question:

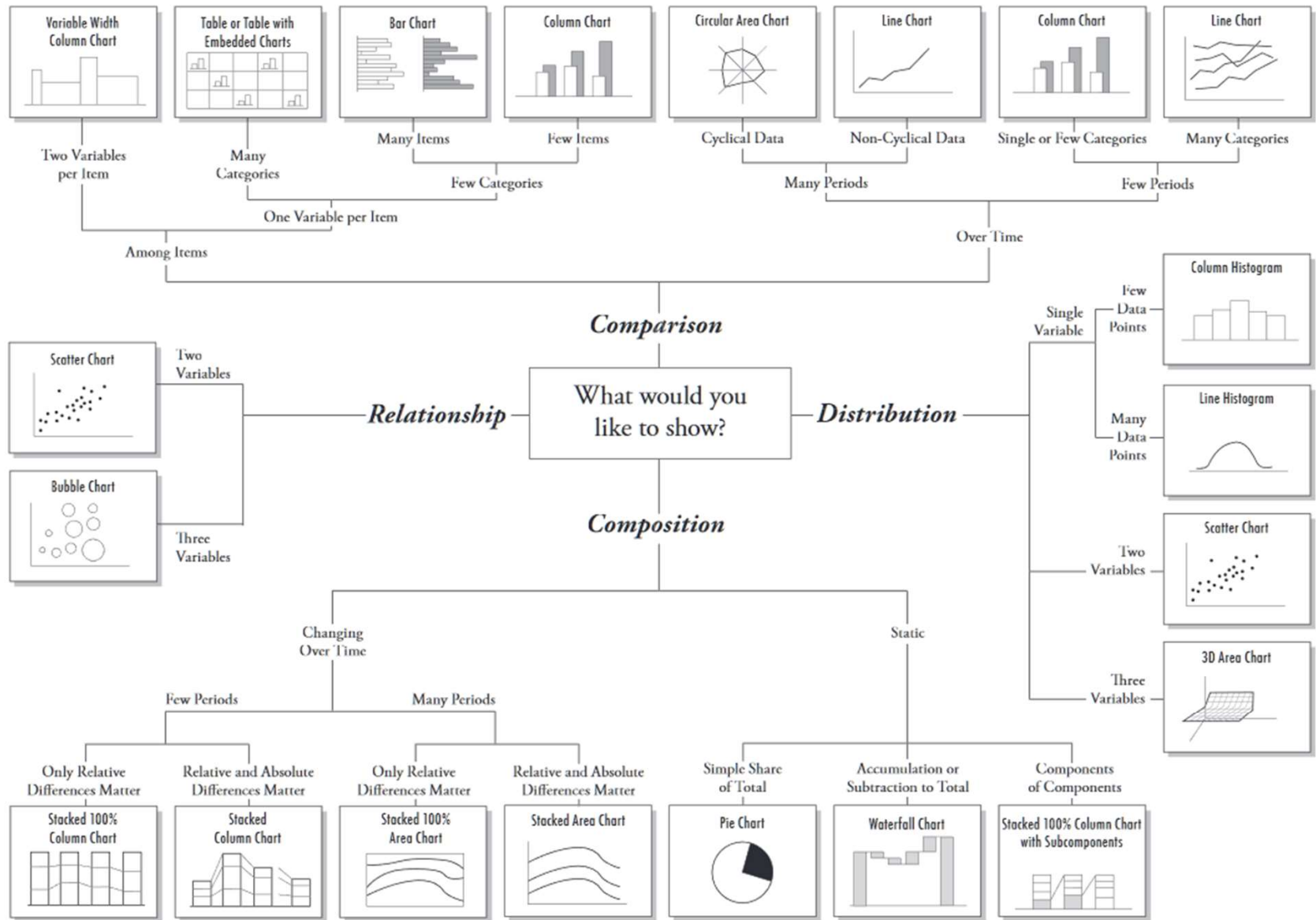
What is the purpose of a data visualization?



## Information Visualization?

- The study of visual representations of data to reinforce human cognition.
- “Help people understand the, structure, relationships meaning in data.”
- Techniques: Charts, Graphs, Maps

# Chart Suggestions—A Thought-Starter



## Review from Weeks 1 & 2

MATLAB has extensive facilities for the plotting of curves and surfaces, and visualization.

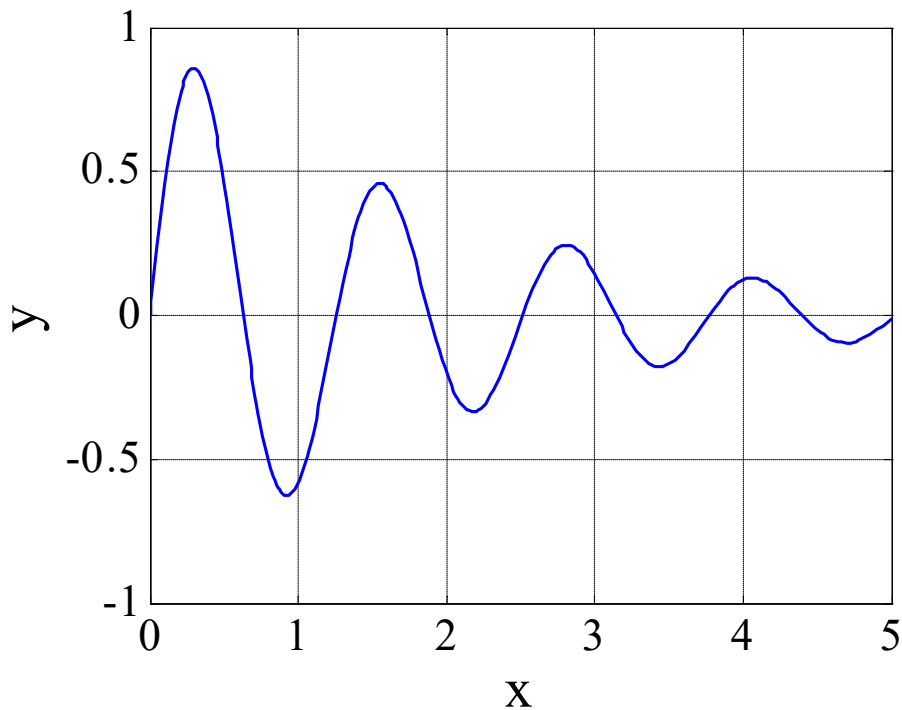
Basic 2D plots of functions and (x,y) pairs can be done with the functions:

`plot`, `fplot`, `ezplot`

```
>> help plot      % 2-D plotting
>> help fplot    % function plotting
>> help ezplot   % easy function plotting
```

If a function  $f(x)$  has already been defined by a function-handle or inline, it can be plotted quickly with **fplot**, **ezplot**, which are very similar. One only needs to specify the plot **range**. For example:

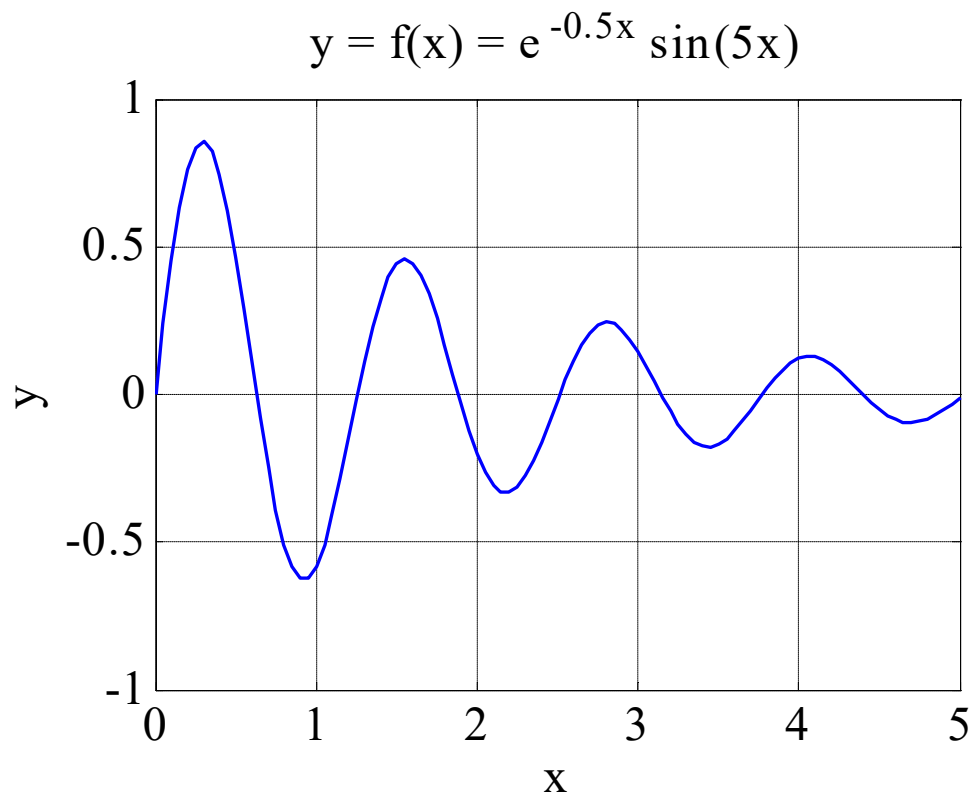
```
>> f = @(x) exp(-0.5*x) .* sin(5*x) ;  
>> fplot(f, [0,5]) ;           % plot over interval [0,5]
```



A **figure window** opens up, allowing further editing of the graph, e.g., adding x,y axis labels, titles, grid, changing colors, and saving the graph in some format, such as WMF, PNG, or EPS, EPSC

using the plot function

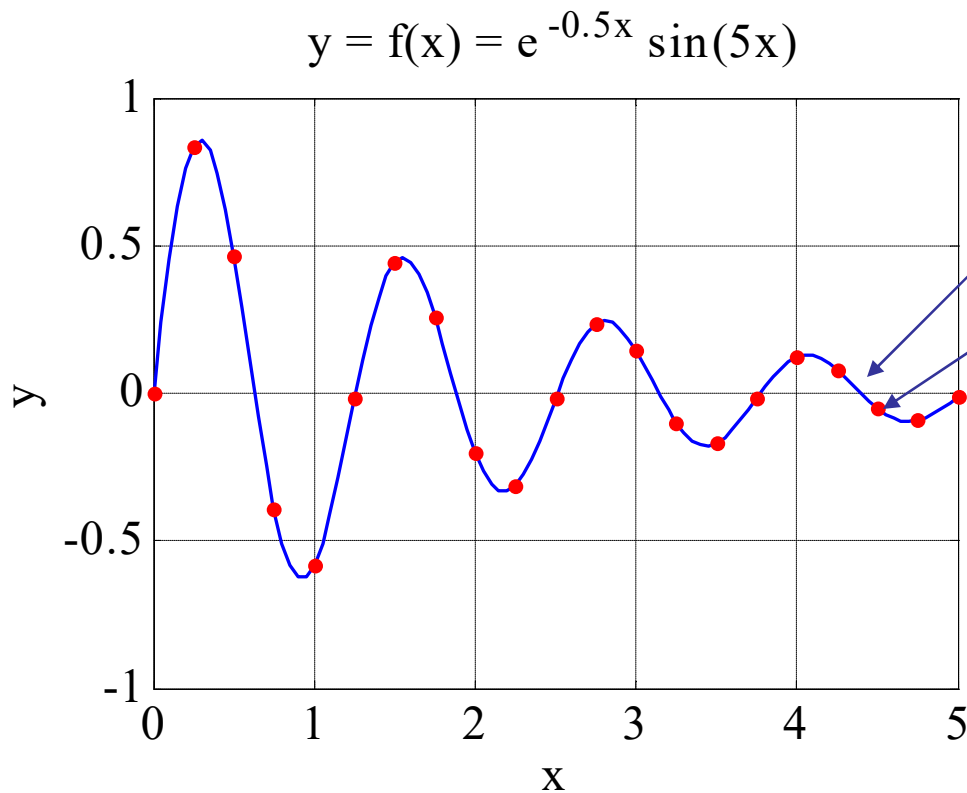
```
>> x = linspace(0,5,101);  
>> y = f(x);  
>> plot(x,y,'b-'); % blue-solid line  
>> xlabel('x'); ylabel('y'); grid;  
>> title('f(x) = e^{-0.5x} sin(5x)');
```



plot annotation can be done by separate commands, as shown above, or from the **plot editor** in the figure window.

## multiple graphs on same plot

```
>> x5 = x(1:5:end); % plot every 5th data point
>> y5 = y(1:5:end);
>> plot(x,y,'b-', x5,y5, 'r. '); % blue-line, red dots
>> xlabel('x'); ylabel('y'); grid;
>> title('f(x) = e^{-0.5x} sin(5x)');
```



(x,y) plotted as blue-solid line

(x5,y5) pairs plotted as red dots

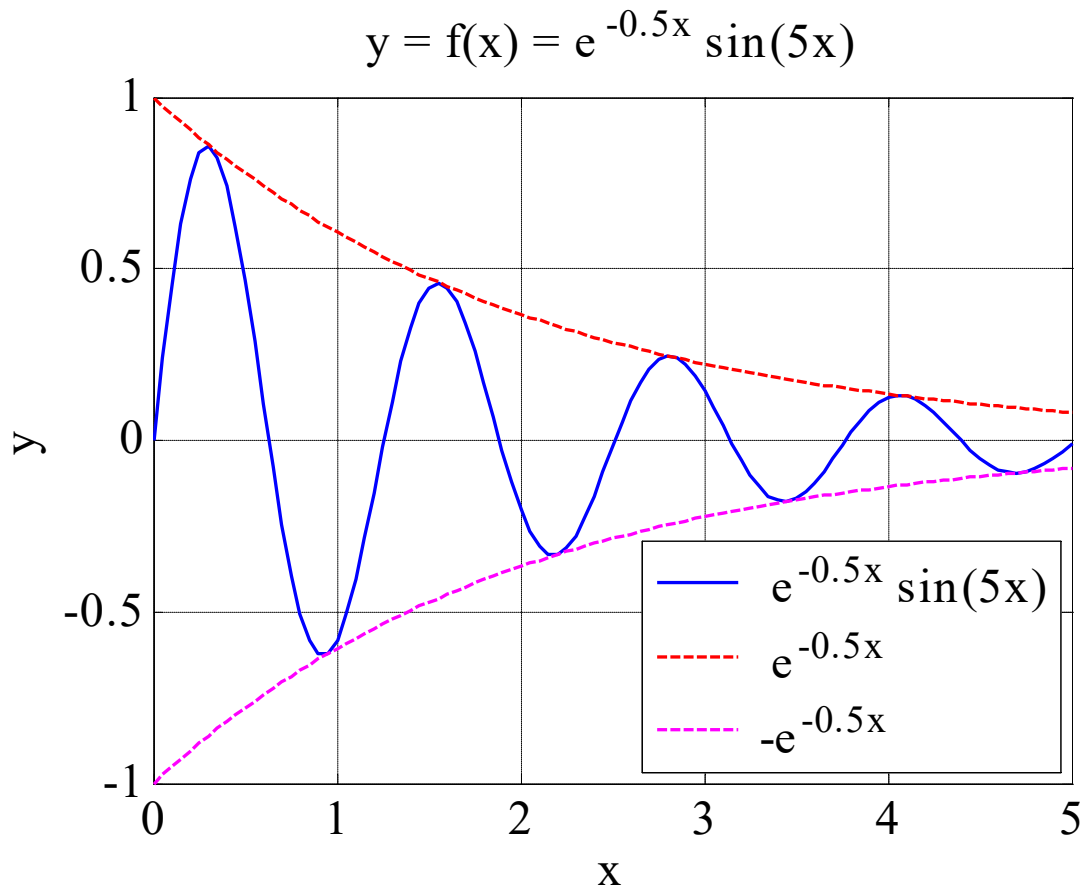
multiple (x,y) pairs---not necessarily of the same size---can be plotted with different line styles.



```

>> ye = exp(-0.5*x);           % envelope of f(x)
>> plot(x,y,'b-', x,ye,'r--', x,-ye,'m--');
>> xlabel('x'); ylabel('y'); grid;
>> title('f(x) = e^{-0.5x} sin(5x)');
>> legend('e^{-0.5x} sin(5x)', 'e^{-0.5x}', ...
        '-e^{-0.5x}', 'location','SE');

```



south-east

ellipsis  
continues to  
next line

plotting multiple curves  
and adding legends

legends can also be  
inserted with plot editor

Multiple plots : use  
"hold on"  
after each plot

# plot

```
plot(x,y, 'specifiers', 'property', prop_value);
```

line style,  
line color,  
marker

line width,  
marker size,  
marker color  
color, marker

Example:

```
plot(x,y, 'b-', 'linewidth', 2, 'markersize', 12, ...  
      'markeredgecolor', 'r', ...  
      'markerfacecolor', 'g');
```

default values:

LineWidth = 0.5 points

MarkerSize = 6

FontSize = 10

## Line Styles, Point Types, Colors, and Properties

Style		Type		Color	
solid	-	point	.	blue	<b>b</b>
dotted	:	circle	o	green	<b>g</b>
dash-dot	- .	x-mark	x	red	<b>r</b>
dashed	--	plus	+	cyan	<b>c</b>
		star	*	magenta	<b>m</b>
		square	s	yellow	<b>y</b>
		diamond	d	black	<b>k</b>
		triang dn	v		
		triangle up	^		
		triang left	<		
		triang right	>		
		pentagram	p		
		hexagram	h		

### property name

linewidth

markersize

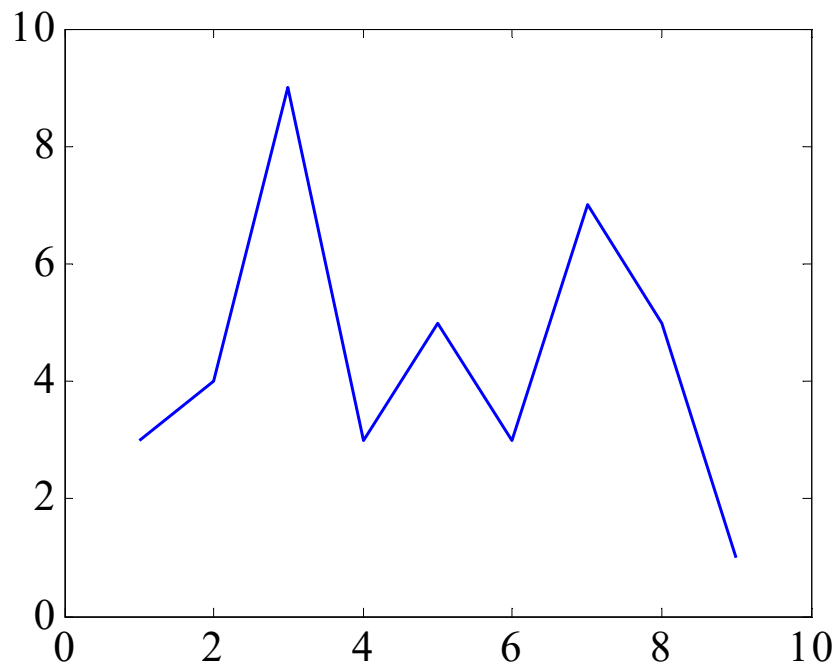
markeredgecolor

markerfacecolor

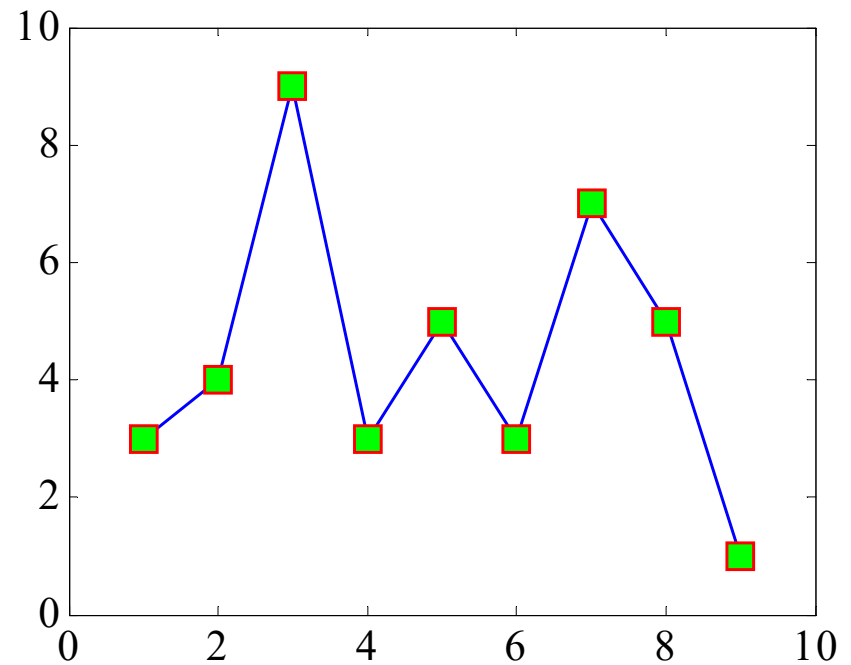
```
x = [1 2 3 4 5 6 7 8 9];  
y = [3 4 9 3 5 3 7 5 1];
```

line styles  
& markers

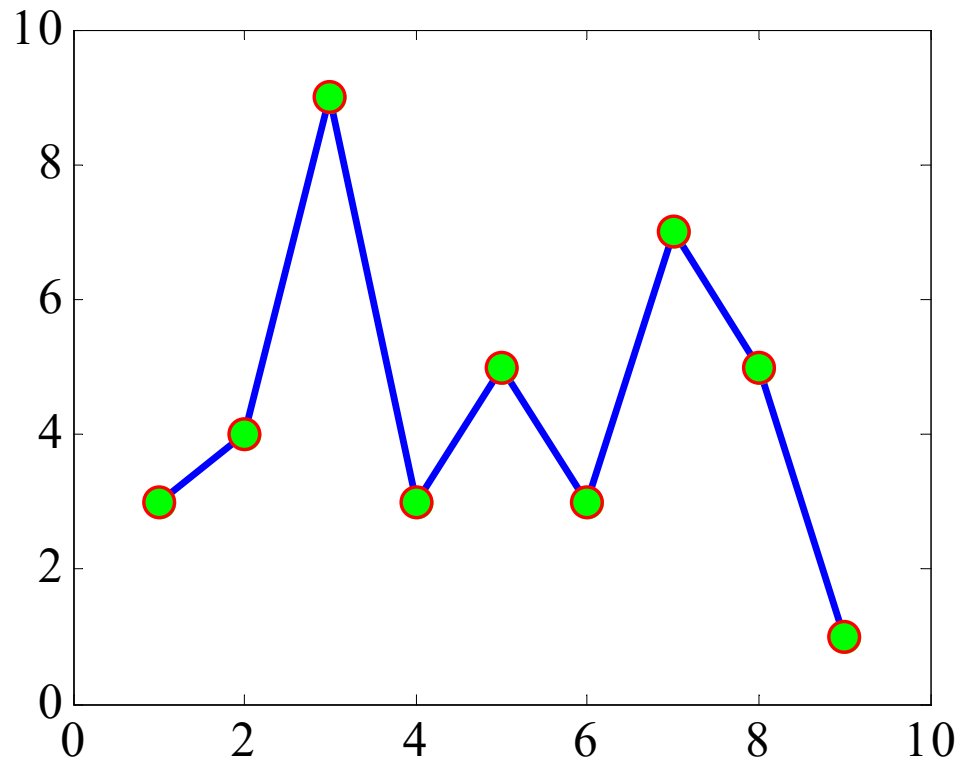
```
plot(x,y,'b-');
```



```
plot(x,y,'bs-', ...  
     'MarkerEdgeColor','r', ...  
     'MarkerFaceColor','g')
```



```
plot(x,y,'b-', 'LineWidth',3);  
hold on;  
plot(x,y,'or', 'MarkerSize', 12, ...  
      'MarkerFaceColor','g');
```



default values

LineWidth = 0.5 points

MarkerSize = 6

FontSize = 10

## plot summary

insert additional option strings

```
plot(x1,y1,'opt1', x2,y2,'opt2', x3,y3,'opt3');
```

**x1,y1** may have different size than **x2,y2**, or **x3,y3**

```
plot(x1,y1,'specs1','prop1',val1);  
hold on;  
plot(x2,y2,'specs2','prop2',val2);  
plot(x3,y3,'specs3','prop3',val3);  
hold off;
```

**hold on/off** allows independent specification of plot parameters

plot variants

`% x = M-vector, Y = MxN matrix`

`plot(x, Y);` ← plot each column of **Y** against **x**

`% X = MxN matrix, Y = MxN matrix`

`plot(X, Y);` ← plot each column of **Y** against each column of **X**

`% Y = MxN real-valued matrix`

`plot(Y);` ← plot **Y** columns against their index

for complex **X, Y** only their real parts are used, and imag parts ignored, exception

`% Z = MxN complex-valued matrix`

`plot(Z);`  
`plot(real(Z), imag(Z));` ← equivalent

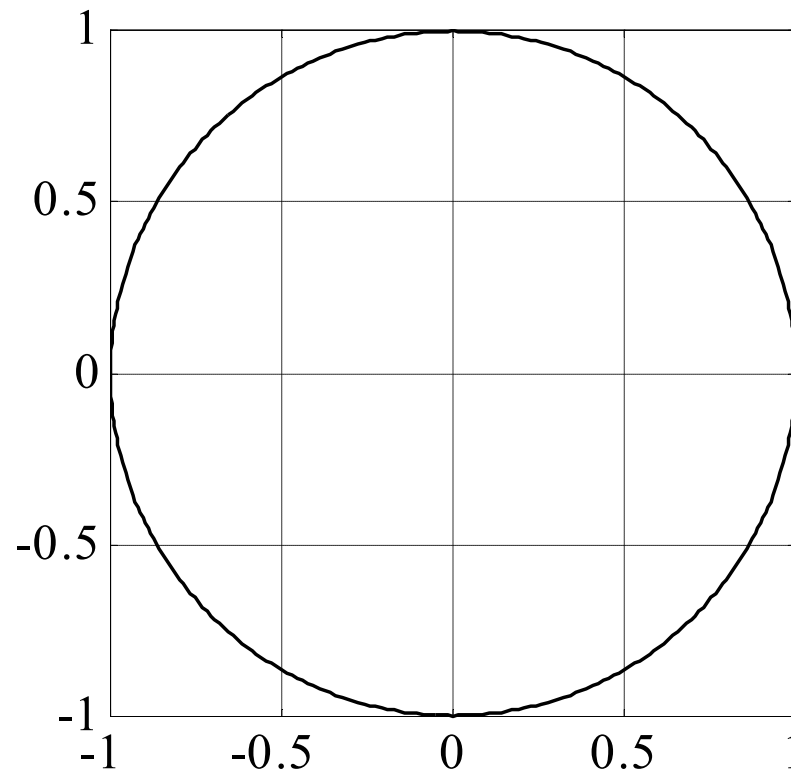
## How to plot a circle

```
theta = linspace(0,2*pi,361);  
z = exp(j*theta);  
figure; plot(z);  
axis equal;  
axis square;  
grid;
```

Euler's formula

$$e^{j\theta} = \cos \theta + j \sin \theta$$

imaginary  
unit,  $j$  or  $i$





## adding text

```
gtext('text_string'); add by mouse  
text(x,y,'text_string','property',value);
```

### property

<b>fontsize</b>	size of text font
<b>color</b>	text color
<b>fontangle</b>	normal, italic
<b>fontweight</b>	normal, bold
<b>backgroundcolor</b>	rectangular area of text
<b>edgecolor</b>	edge of rectangular box
<b>linewidth</b>	rectangular box
<b>rotation</b>	text orientation
<b>fontname</b>	specify font

properties can  
also be set with  
the plot editor

can also be used in **title**, **xlabel**, **ylabel**, **legend**

adding text

```
x = linspace(0,pi,100); y = sin(x);
```

```
plot(x/pi,y,'b','linewidth',2);
```

```
xlabel('{\itx}/\pi'); grid on;
```

```
str = 'max at {\itx} = \pi/2';
```

```
gtext(str,'fontsize',20);
```

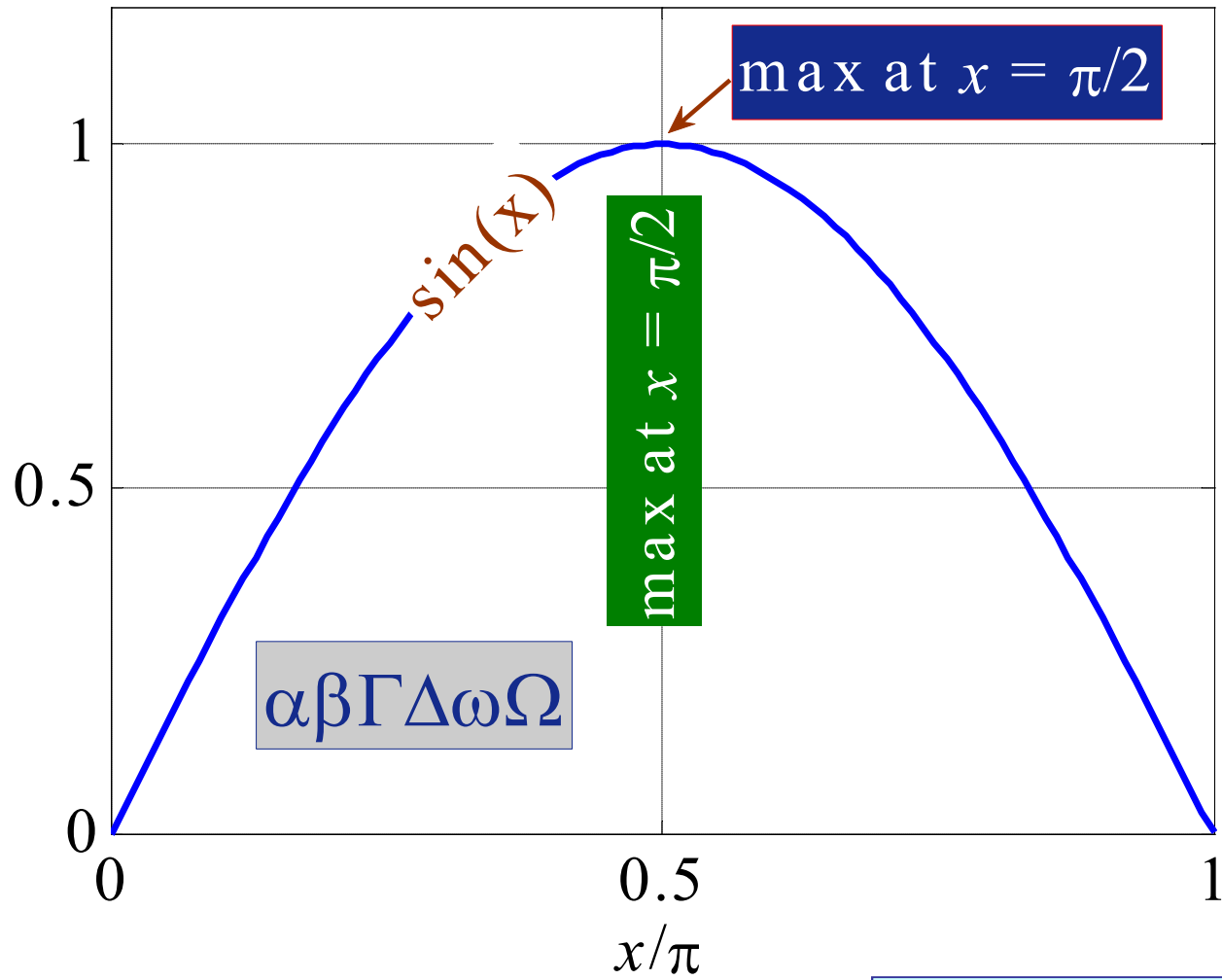
```
gtext(str,'fontsize',20,'rotation',90);
```

```
gtext('sin(x)','fontsize',20,'rotation',60);
```

```
gtext('\alpha\beta\Gamma\Delta\omega\Omega');
```

text positions, colors, sizes, and background colors  
can be fine-tuned from the plot editor (see net page)

adding text



find out the  $[x,y]$  coordinates  
of a point using


```
[x,y] = ginput;
```

## axis settings

```
axis auto;           % default settings
axis equal;         % equal x,y units
axis square;       % square box
axis off;          % remove axes
axis on;           % restore axes
axis tight;        % limits from data range
axis ij;           % matrix mode (i=vert, j=horiz)
axis xy;           % cartesian mode
axis normal;       % default axis
```

```
axis ([xmin,xmax,ymin,ymax]);           % limits
axis ([xmin,xmax,ymin,ymax,zmin,zmax]);
```

```
xlim([xmin,xmax]);           % set x-axis limits
ylim([ymin,ymax]);
zlim([zmin,zmax]);
```

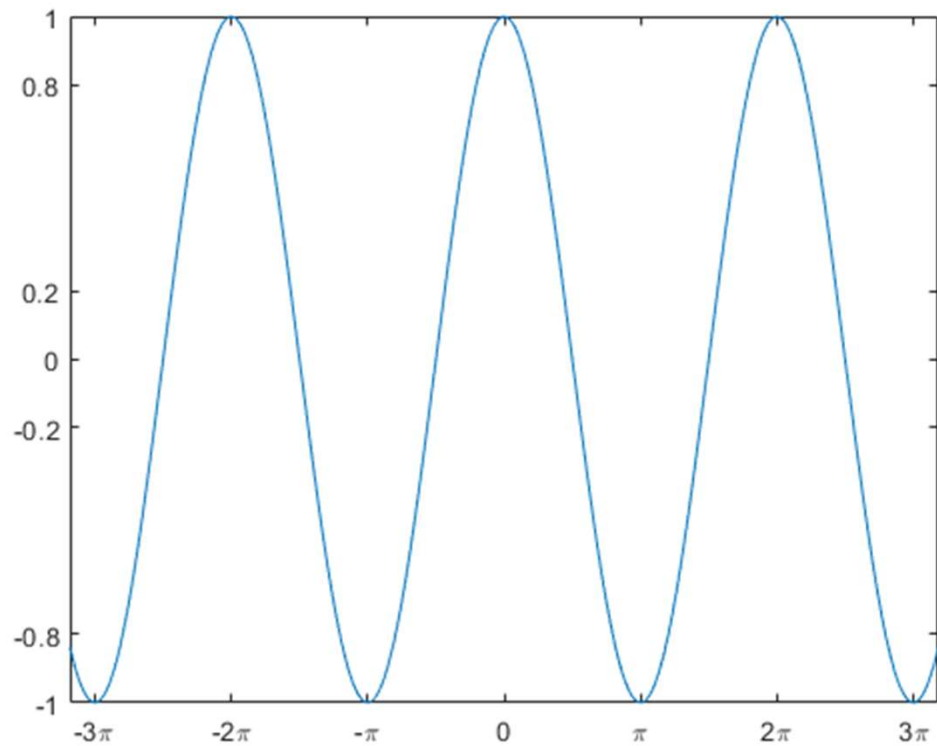


correlated

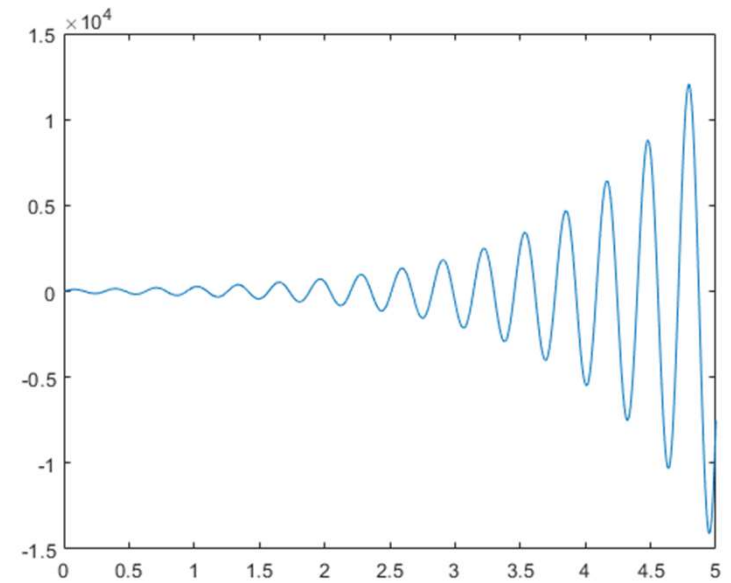
```
set(gca, 'xtick', v);       % v = tickmark vector
set(gca, 'ytick', v);       % e.g., v = 0:2:10
```

```
x = linspace(-10,10,200);  
y = cos(x);  
plot(x,y)
```

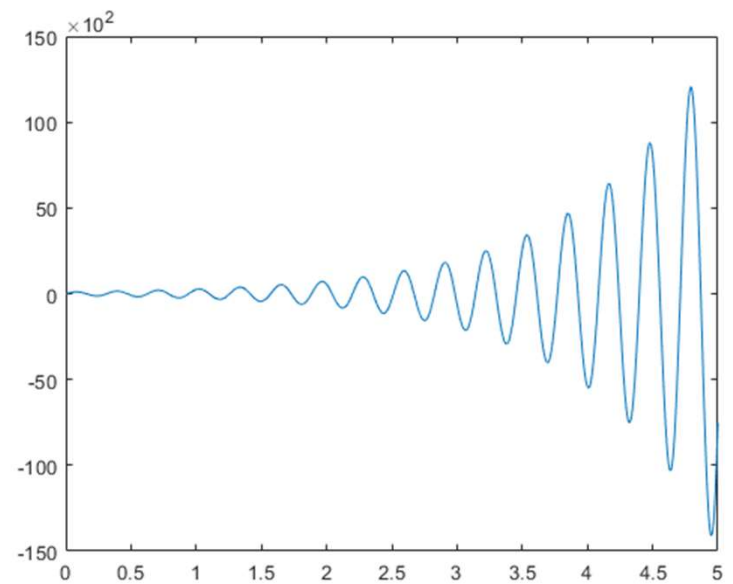
```
xticks([-3*pi -2*pi -pi 0 pi 2*pi 3*pi])  
xticklabels({'-3\pi', '-2\pi', '-\pi', '0', '\pi', '2\pi', '3\pi'})  
yticks([-1 -0.8 -0.2 0 0.2 0.8 1])
```



```
x = linspace(0,5,1000);  
y = 100*exp(x).*sin(20*x);  
plot(x,y)
```



```
ax = gca;  
ax.YAxis.Exponent = 2;
```

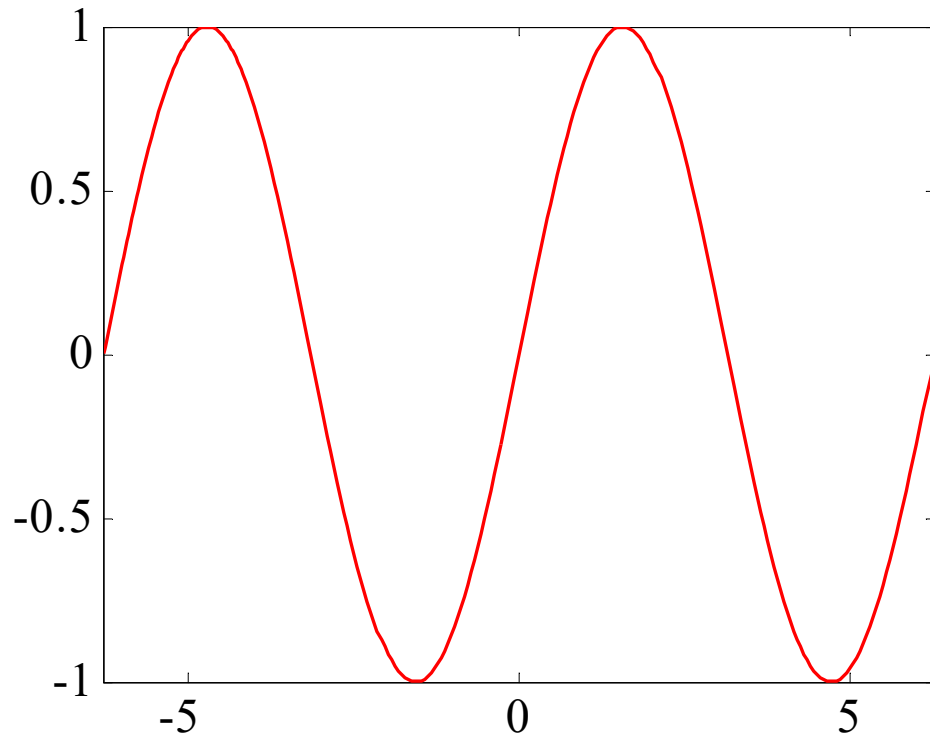


## 2D plotting functions

<code>plot</code>	basic x-y plot
<code>fplot</code>	function plot
<code>ezplot</code>	function plot
<code>loglog</code>	log x,y axes
<code>semilogx</code>	log x-axis
<code>semilogy</code>	log y-axis
<code>plotyy</code>	left & right y-axes
<code>polar</code>	polar plot
<code>ezpolar</code>	polar
<code>comet</code>	animated x-y plot
<code>errorbar</code>	plot with error bars
<code>stem,stairs</code>	stem and staircase
<code>scatter</code>	scatter plot
<code>bar,barh</code>	bar graphs
<code>pie</code>	pie chart
<code>hist</code>	histogram
<code>fill,area</code>	polygon & area fill

## fplot, ezplot

```
fplot(@sin, [-2,2]*pi);  
fplot('sin', [-2,2]*pi);  
fplot('sin(x)', [-2,2]*pi);  
f = @(x) sin(x);  
fplot(f, [-2,2]*pi);
```



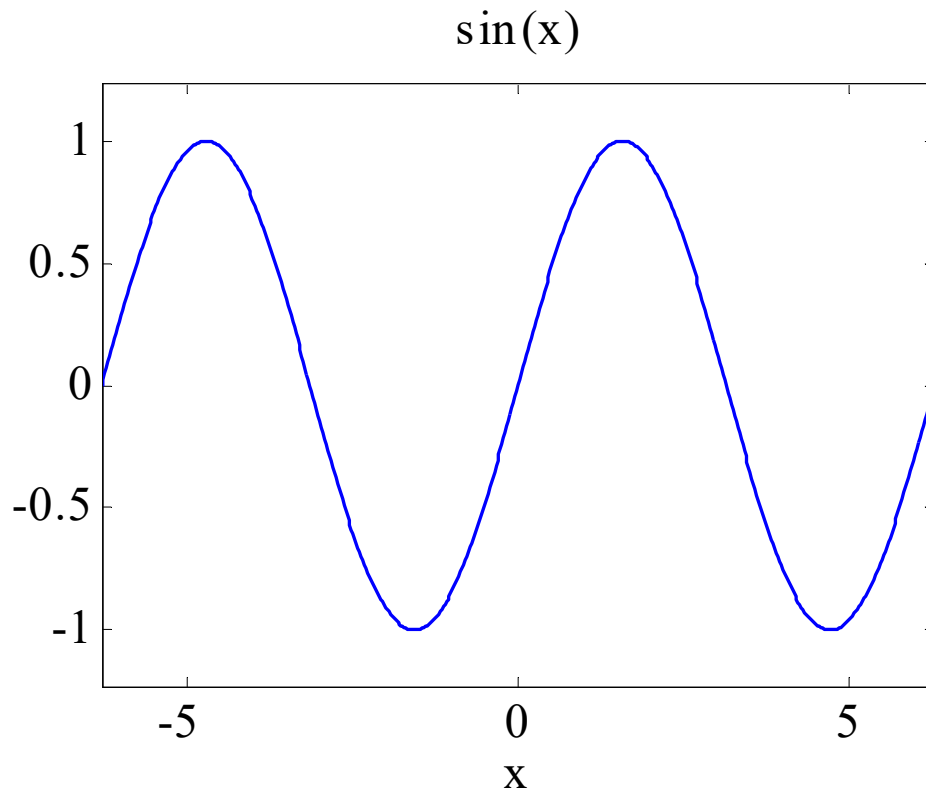
linestyles & colors  
can be changed from  
the figure window, or

↓  
`fplot(f, [-2,2]*pi, 'r');`



## fplot, ezplot

```
ezplot(@sin, [-2,2]*pi);  
ezplot('sin', [-2,2]*pi);  
ezplot('sin(x)', [-2,2]*pi);  
f = @(x) sin(x);  
ezplot(f, [-2,2]*pi);
```



linestyles & colors  
can be changed from  
the figure window

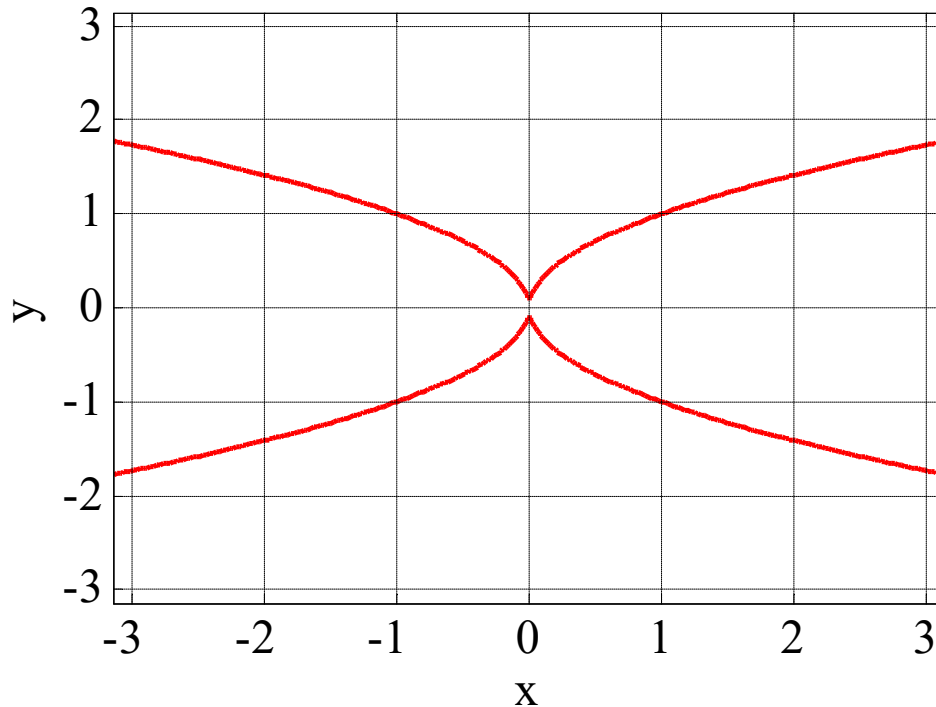
fplot, ezplot

```
ezplot('x^2-y^4', [-pi,pi]);
```

```
f = @(x,y) x.^2 - y.^4;
```

```
ezplot(f, [-pi,pi]);
```

$$x^2 - y^4 = 0$$



ezplot can plot functions defined implicitly, i.e.,  $f(x,y) = 0$

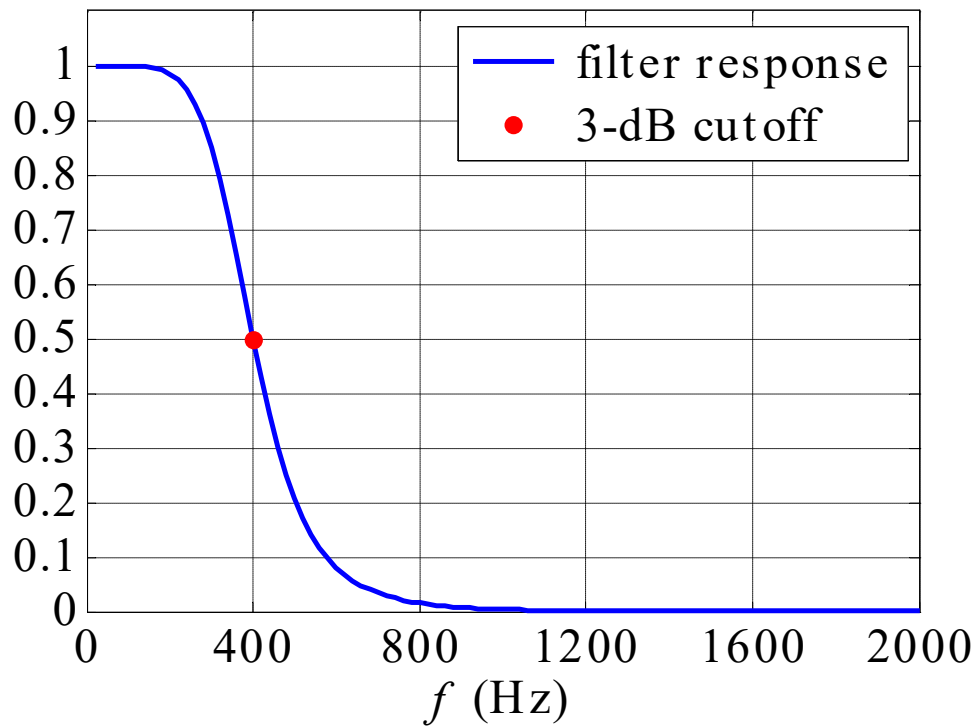
fplot plots function with single variable

## loglog plots

## Butterworth lowpass audio filter

$$|H(f)|^2 = \frac{1}{1 + \left(\frac{f}{f_0}\right)^{2N}}$$

low pass filter



$$N = 3$$
$$f_0 = 400 \text{ Hz}$$

$$10 \cdot \log_{10}(0.5) = -3.01 \text{ dB}$$

```
f = linspace(20,2000,100);    % 20 Hz to 2 kHz
f0 = 400;                    % 3-dB frequency

H2 = 1./(1+ (f/f0).^6);      % magnitude square

plot(f,H2,'b', 'linewidth',2);
hold on;
plot(f0,0.5,'r.', 'markersize',20);

axis(0,2000, 0:400:2000);
yaxis(0,1.1, 0:0.1:1); grid;
xlabel('{\itf} (Hz)');
title('low pass filter');

legend(' filter response', ' 3-dB cutoff',...
'location', 'ne');
```

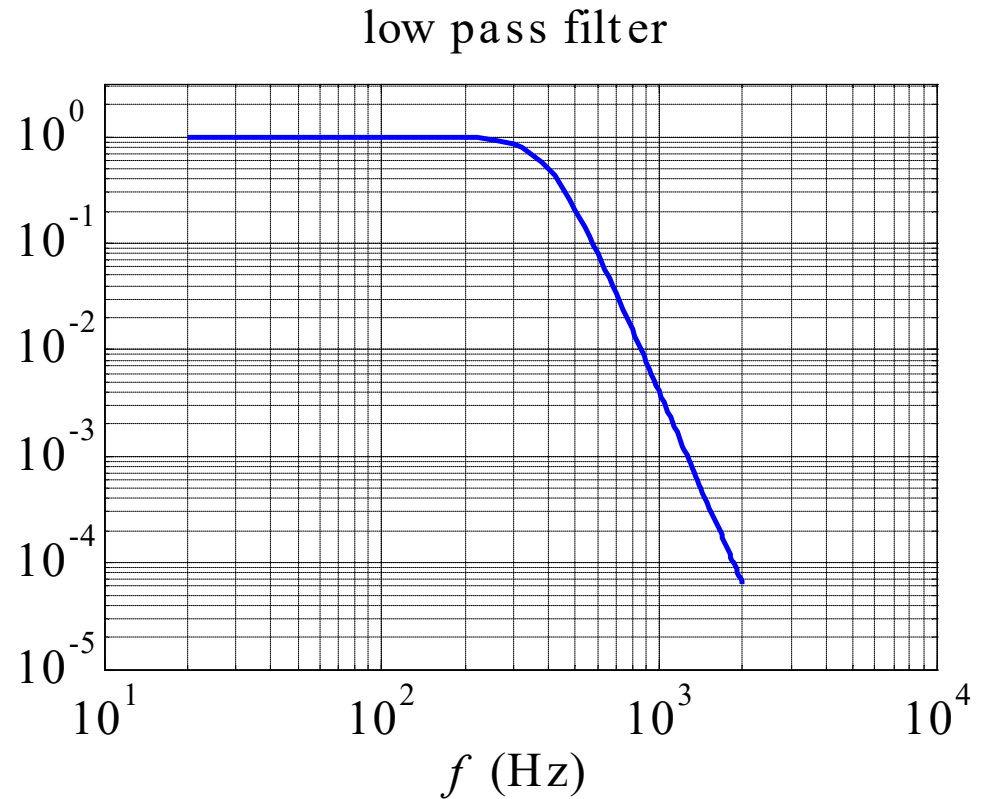
## loglog

```
loglog(f,H2, 'b', 'linewidth',2);
```

```
yaxis(10^(-5), 10^(0.5), 10.^(-5:0));
```

```
xlabel('\itf (Hz)'); grid;
```

```
title('low pass filter');
```



`semilogy(x1,r1,...)` plots all  $r_n$  versus  $x_n$  pairs. If only one of  $x_n$  or  $r_n$  is a matrix,

## semilogy

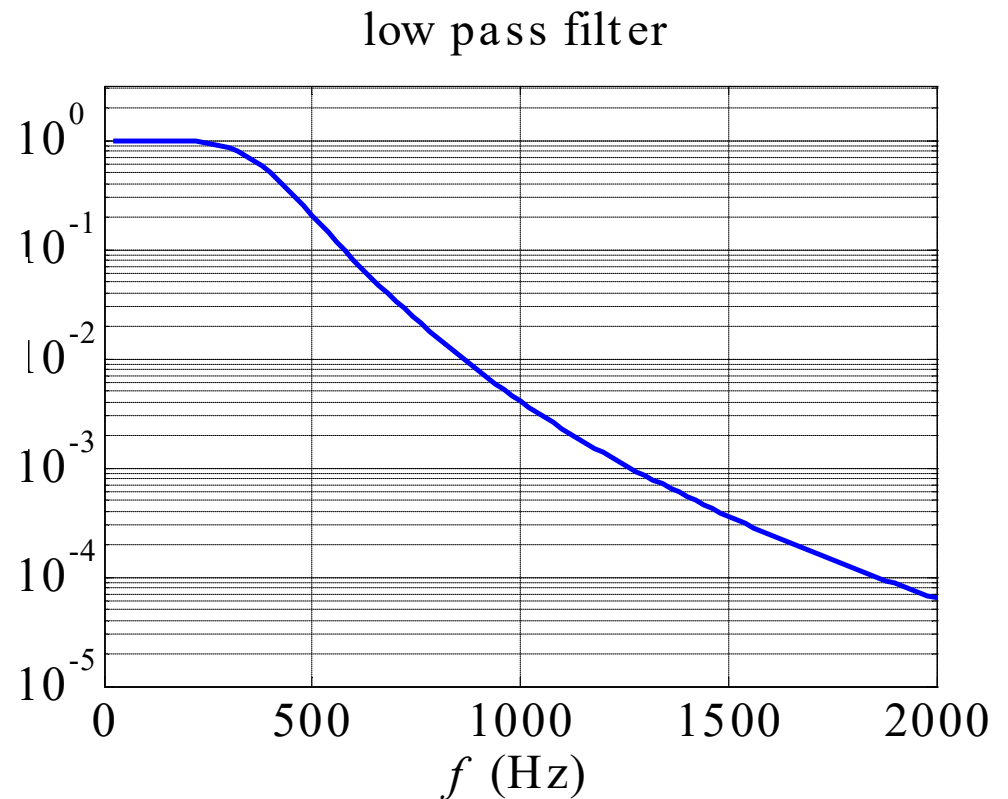
```
semilogy(f,H2, 'b', 'linewidth',2);
```

```
yaxis(10^(-5), 10^(0.5), 10.^(-5:0));
```

```
xlabel('\itf (Hz)'); grid;
```

```
title('low pass filter');
```

`semilogy`  
creates a plot using a base  
10 logarithmic scale

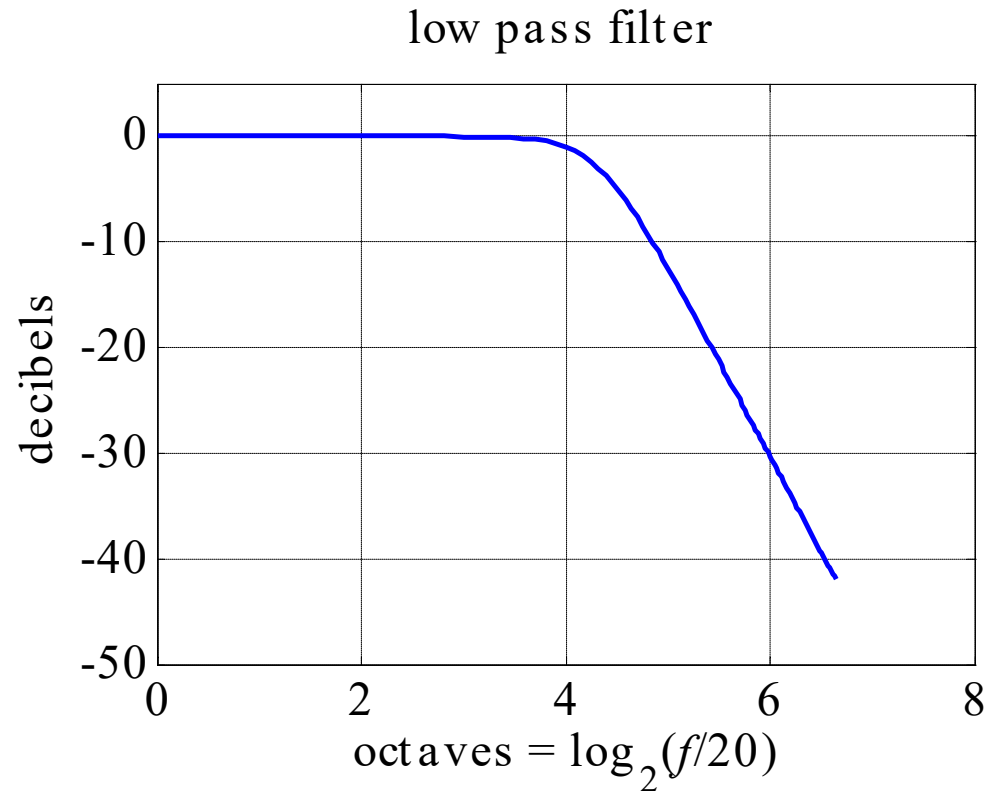


```
plot(log2(f/20), 10*log10(H2), 'b');
```

```
xaxis(0,8, 0:2:8); yaxis(-50,5,-50:10:0);  
xlabel('octaves = log_2({\itf}/20)');  
ylabel('decibels'); grid;  
title('low pass filter');
```

dB vs. octaves

filter gain in dB  
 $10 \log_{10} (|H(f)|^2)$



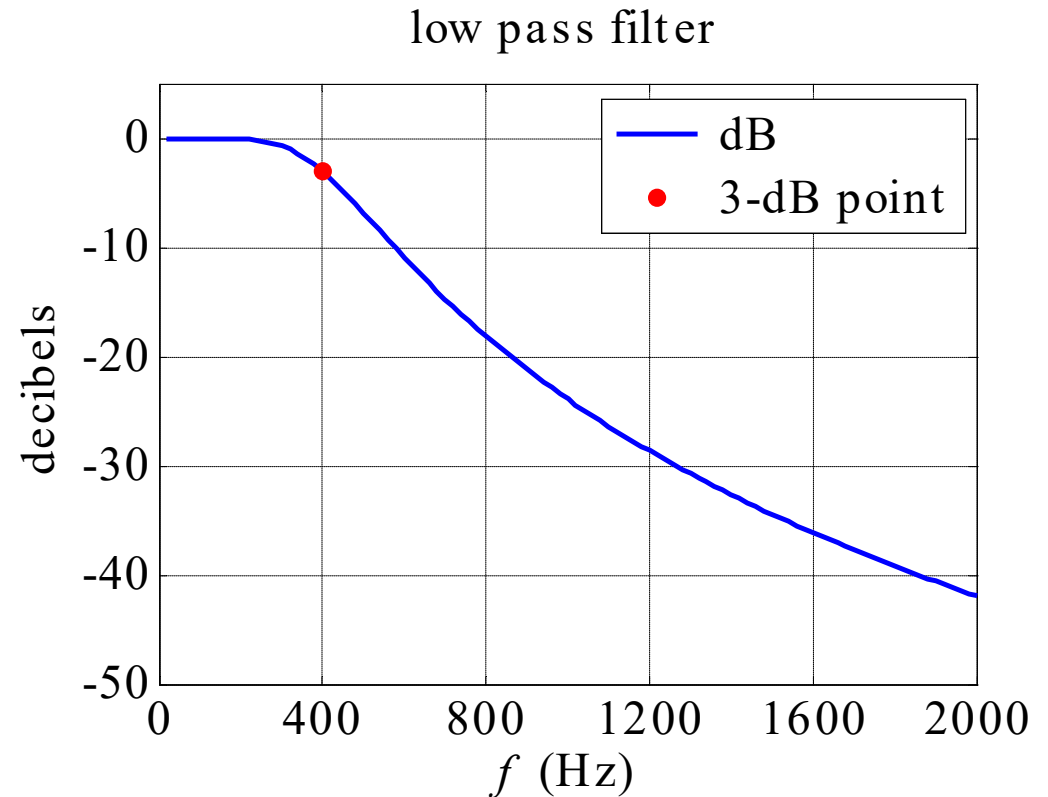
```

plot(f, 10*log10(H), 'b', 'linewidth',2);
hold on; plot(f0,10*log10(0.5), 'r.', ...
'markersize',20);

axis(0,2000, 0:400:2000); yaxis(-50,5,-50:10:0);
xlabel('\itf (Hz)'); ylabel('decibels'); grid;
title('low pass filter');
legend(' dB', ' 3-dB point',...
'location', 'ne');

```

dB vs. Hz





## semilogy example – Moore's law

```
Y = load('transistor_count.dat'); % file on webpage

y = Y(:,1); % transistor count
t = Y(:,2); % year

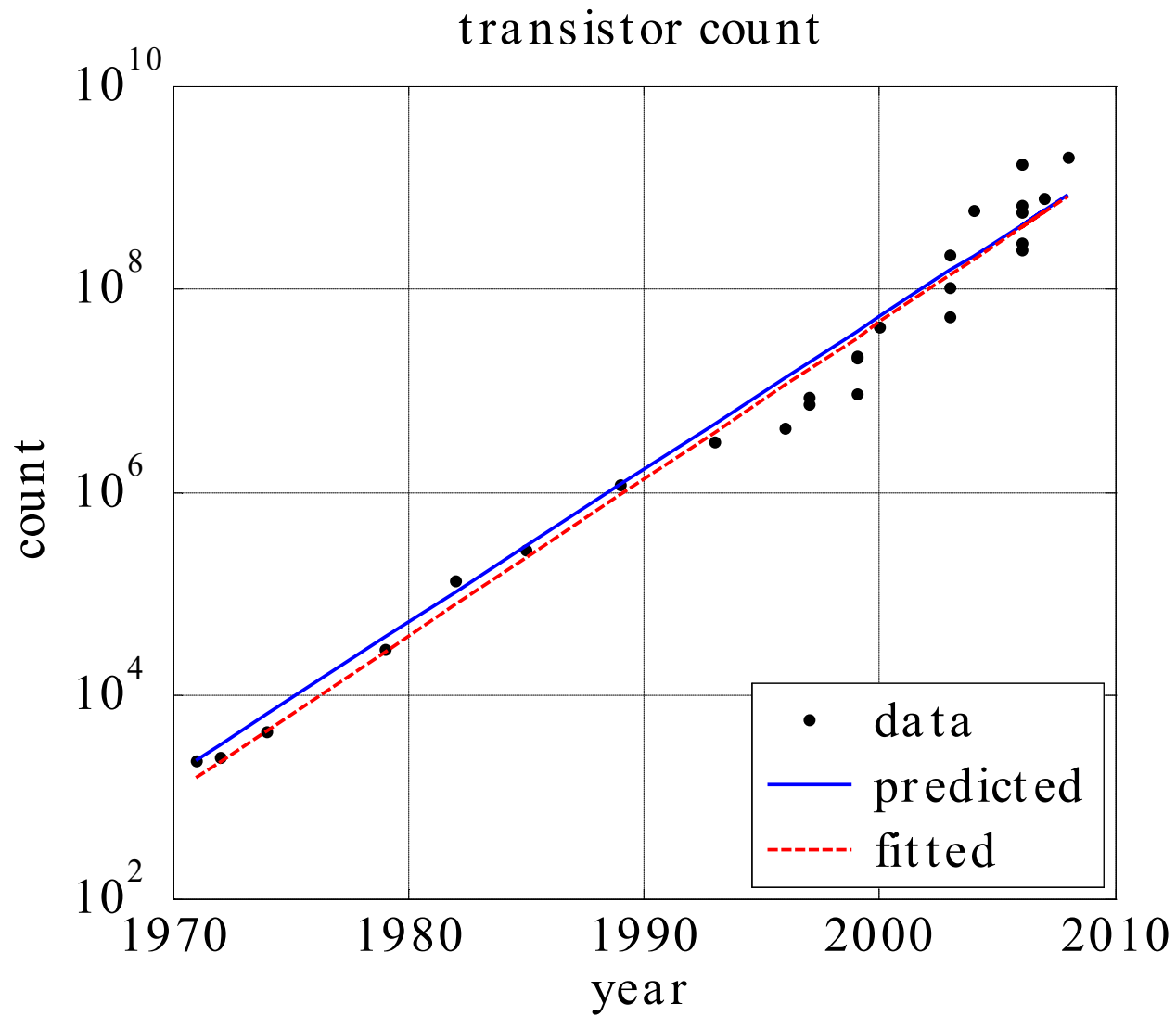
c1 = y(1); % c1 = 2300, starting count
t1 = t(1); % t1 = 1971, starting year

c = c1 * 2.^((t-t1)/2); % predicted count

a = 1540.1813; b = 0.5138; % least-squares fit
f = a * 2.^(b*(t-t1)); % fitted curve

figure;
semilogy(t,y,'k.', t,c,'b-', t,f,'r--');
xlabel('year'); ylabel('count');
title('transistor count');
legend(' data', ' predicted', ' fitted',...
       'location','se');
```

# semilogy example – Moore's law



## 3d order Butterworth lowpass filter

Ploty:

Create graph with two y-axes

frequency response

$$H(f) = \frac{1}{(1 + s)(1 + s + s^2)}, \quad s = \frac{jf}{f_0}$$

imaginary unit

$$G(f) = 10 \log_{10}(|H(f)|^2) \quad \leftarrow \text{magnitude response (dB)}$$

$$\theta(f) = -\text{Arg}(H(f)) \quad \leftarrow \text{phase response (radians)}$$

$$|H(f)|^2 = \frac{1}{1 + (f/f_0)^6} \quad \leftarrow \text{magnitude response in absolute units}$$

## plotyy

```
f = linspace(20,2000,100); f0 = 400; s = j*f/f0;
H = 1./((1+s).*(1 + s + s.^2));
G = 10*log10(abs(H).^2);
th = angle(H) * 180/pi;%convert radian to degrees

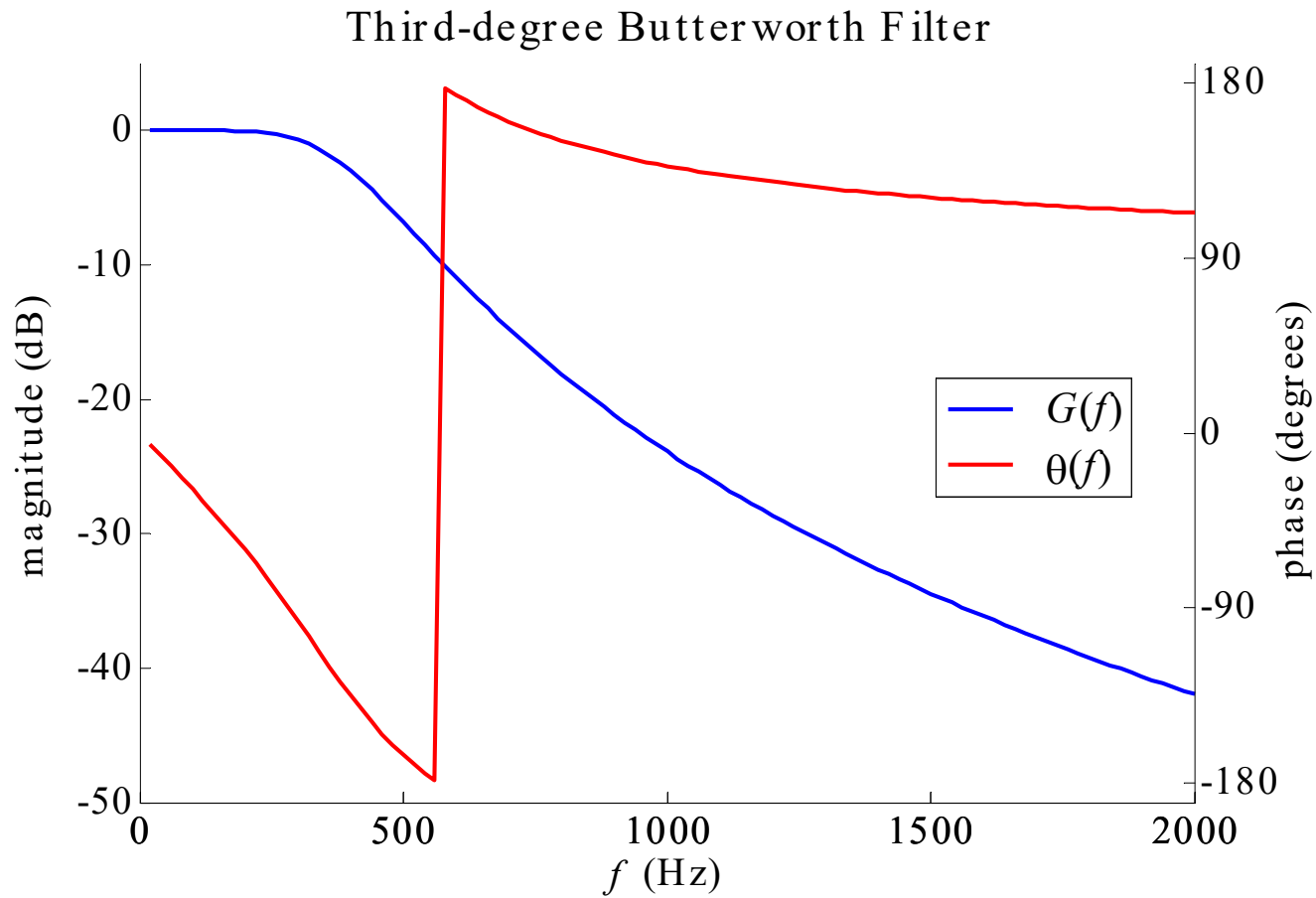
[a,h1,h2] = plotyy(f,G, f,th);
xlabel('\itf (Hz)');
axes(a(1));
yaxis(-50,5, -50:10:0);
ylabel('magnitude (dB)');
axes(a(2));
yaxis(-190,190, -180:90:180);
ylabel('phase (degrees)');

set(h1, 'linewidth',2, 'color', 'b');
set(h2, 'linewidth',2, 'color', 'r');
legend([h1,h2], ' G(f)', ' \theta(f)');
```

**a=[a(1),a(2)],h1,h2**  
are axis and line handles,

**axes** activates left, then  
right axis

set line properties



title, x-y axis labels, linestyle, colors, legends, and tickmarks can also be set from the figure window (select **left** or **right** y-axis from the plot browser)

## scatter plots

```
scatter(x,y, area, color);
```

```
plot(x,y, '.');
```

similar to this,

but **scatter** allows more control  
of the area and color of dots

```
>> help scatter  
>> doc scatter
```

```

N=10000; rng(101);
x = pi * rand(1,N);
y = rand(1,N);

i = find(y < sin(x));
j = find(y > sin(x));

scatter(x(i),y(i),1,'r');
hold on;
scatter(x(j),y(j),1,'b');

x = linspace(0,pi,100);
y = sin(x);
plot(x,y,'r-');

A = length(i)/N * pi

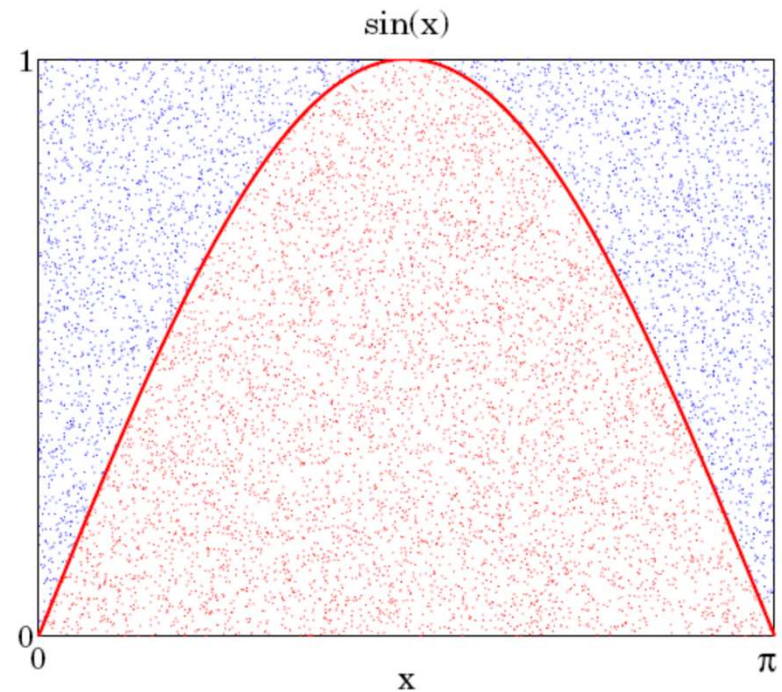
```

```

A =
    1.9915

```

Example of a Monte Carlo calculation of the area under the curve:  $\sin(x)$ ,  $0 \leq x \leq \pi$   
actual area is:  $A = 2$



estimated area is the rectangular area times the fraction of the  $(x,y)$  pairs lying under the curve

## subplots

3 x 4 pattern

general syntax:

```
subplot(n,m,p) ;
```

**n x m** = box pattern

**p** = counting figures  
across rows

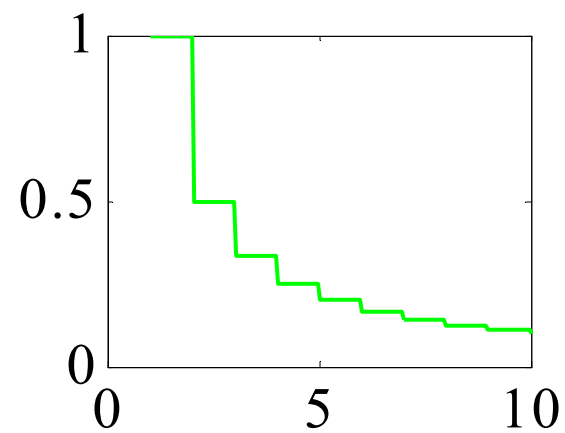
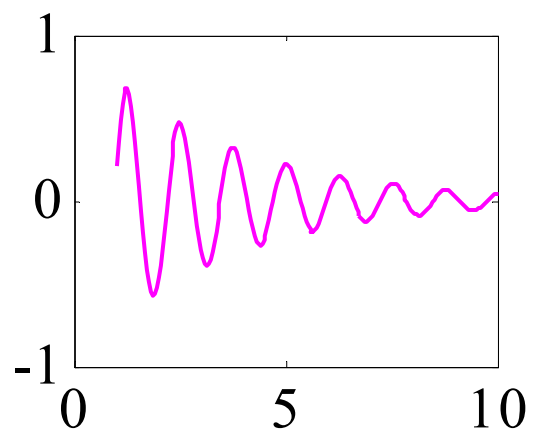
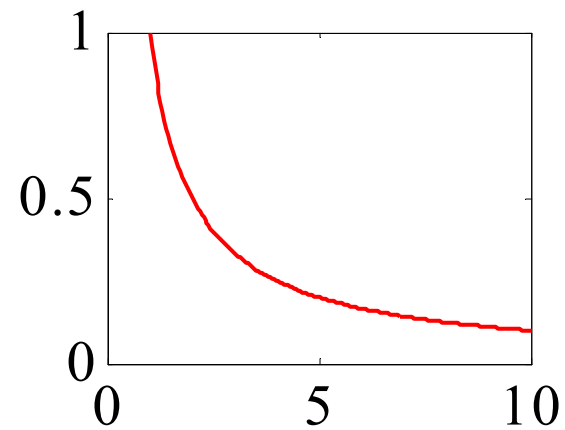
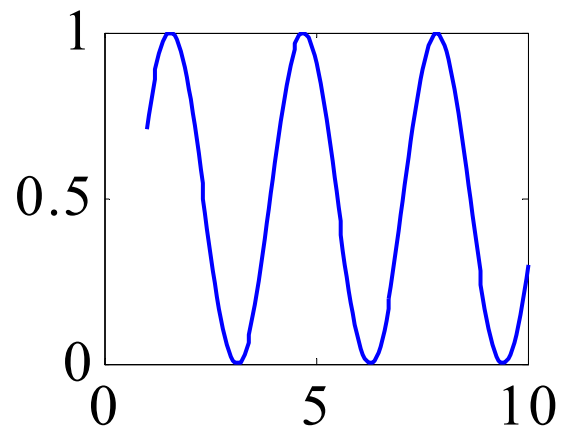
1	2	3	4
5	6	7	8
9	10	11	12

```
subplot(3,4,1)  
subplot(3,4,2)  
etc.
```

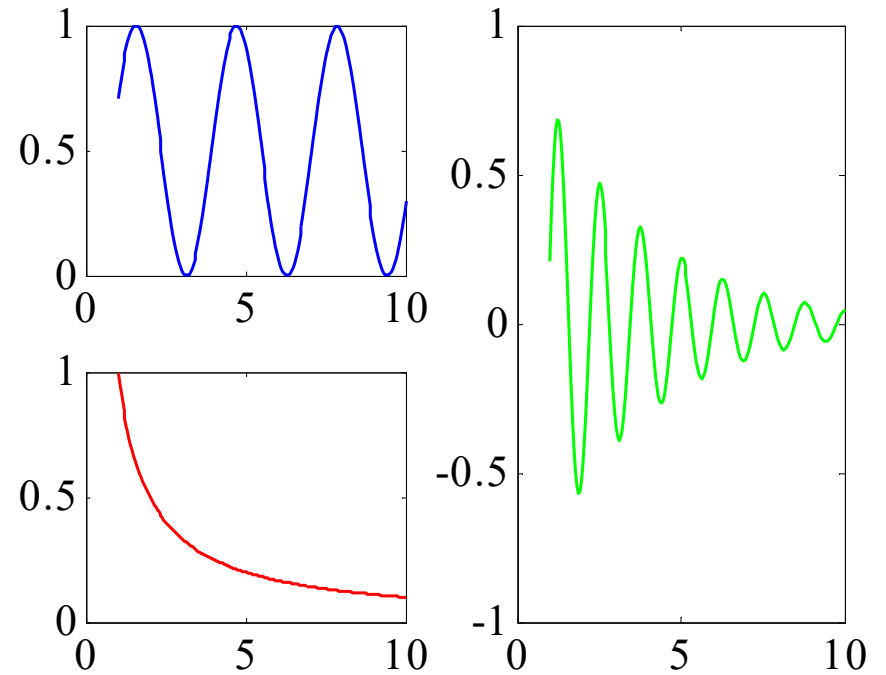
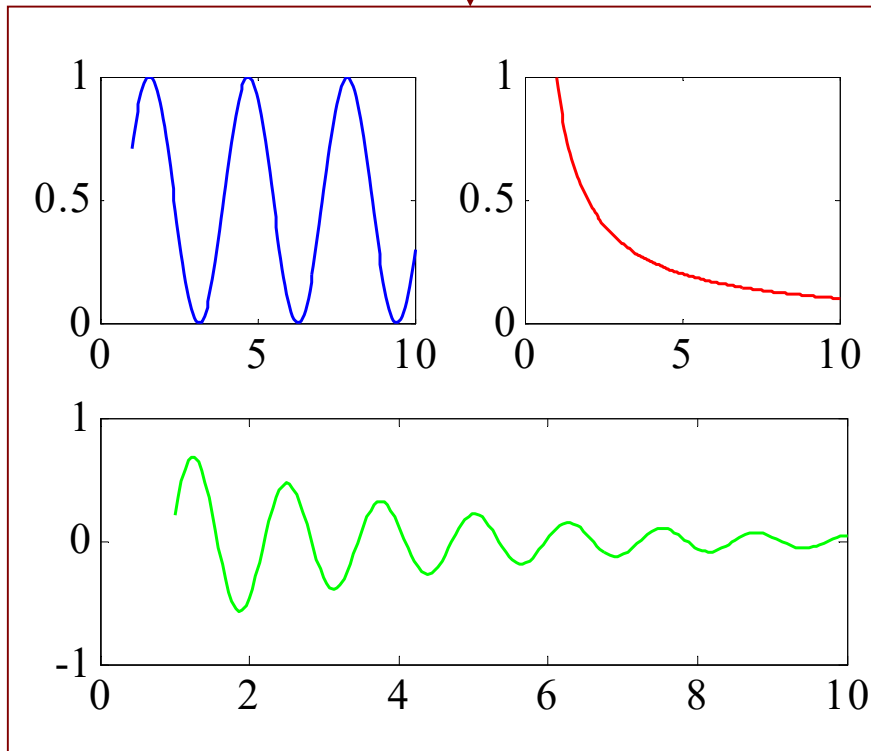
```
x = linspace(1,10,200) ;  
y1 = sin(x).^2 ;  
y2 = 1./x ;  
y3 = exp(-0.3*x). *cos(5*x) ;  
y4 = 1./floor(x) ;
```



```
subplot(2,2,1); plot(x,y1,'b');  
subplot(2,2,2); plot(x,y2,'r');  
subplot(2,2,3); plot(x,y3,'m');  
subplot(2,2,4); plot(x,y4,'g');
```



```
subplot(2,2,1); plot(x,y1,'b');  
subplot(2,2,2); plot(x,y2,'r');  
subplot(2,1,2); plot(x,y3,'g');
```

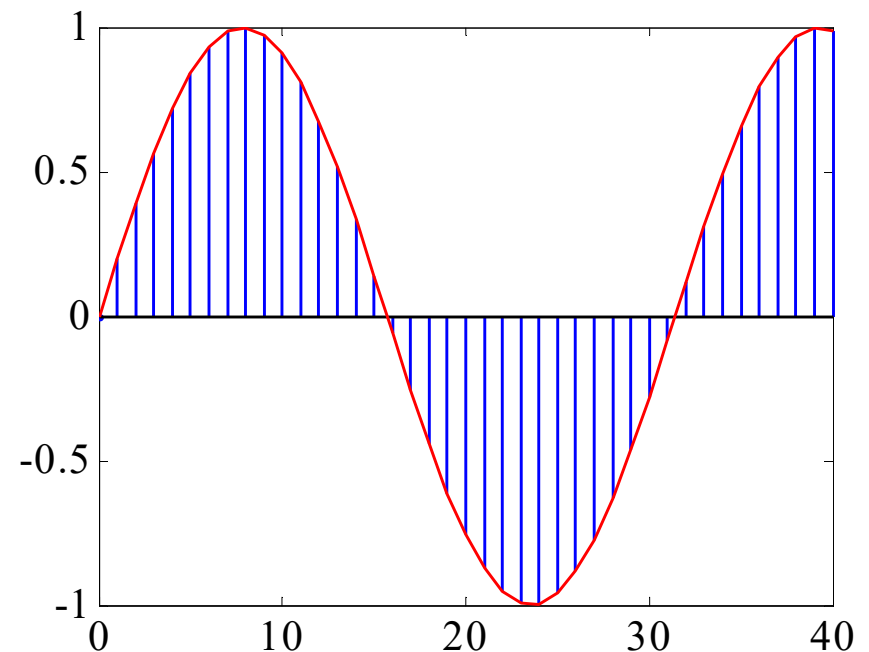
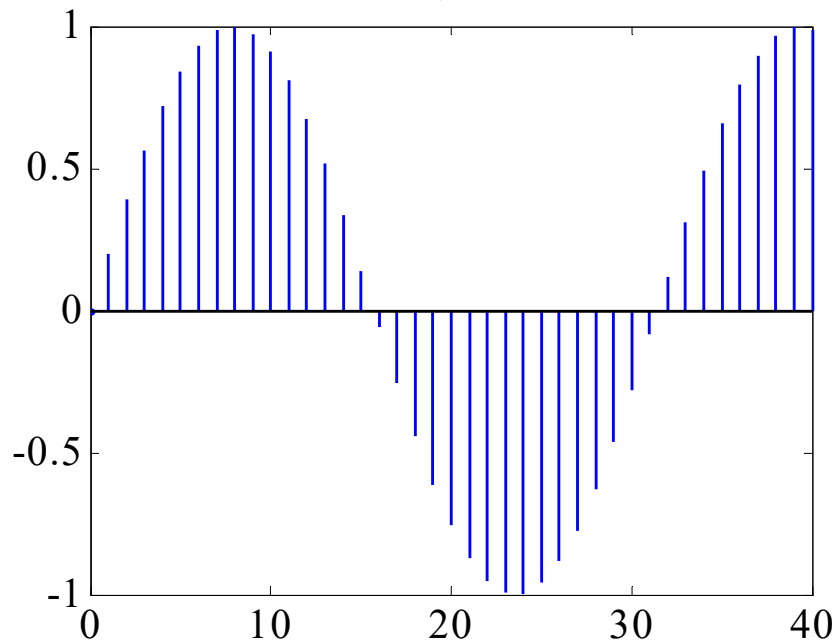


```
subplot(2,2,1); plot(x,y1,'b');  
subplot(2,2,3); plot(x,y2,'r');  
subplot(1,2,2); plot(x,y3,'g');
```

```
x = linspace(0,40,41);  
y = sin(x/5);  
stem(x,y,'b','marker','none');
```

## stem plots

Plot discrete  
sequence data

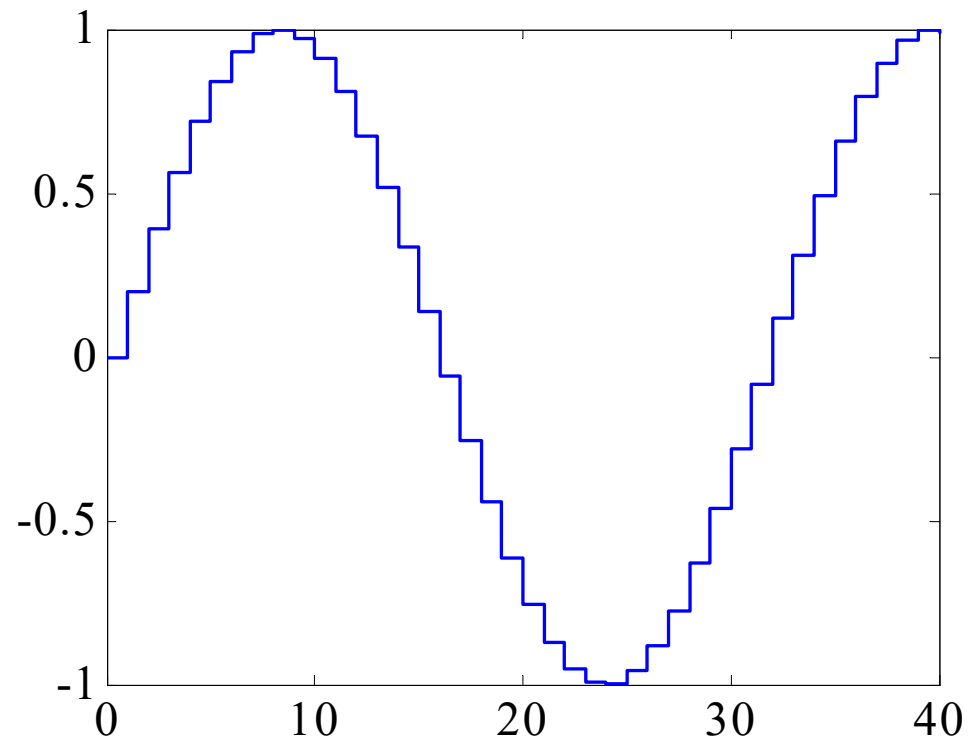


useful for displaying  
discrete-time signals  
in DSP applications

```
stem(x,y,'b','marker','none');  
hold on; plot(x,y,'r-');
```

stairs

```
x = linspace(0,40,41);  
y = sin(x/5);  
stairs(x,y,'b');
```



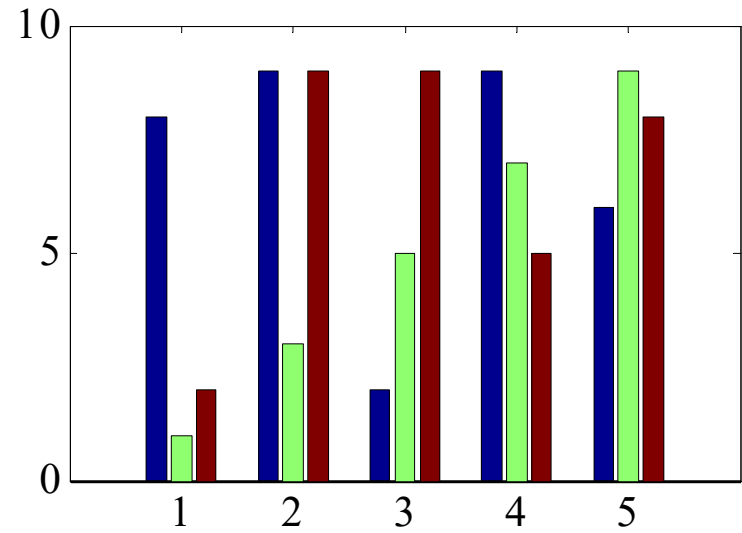
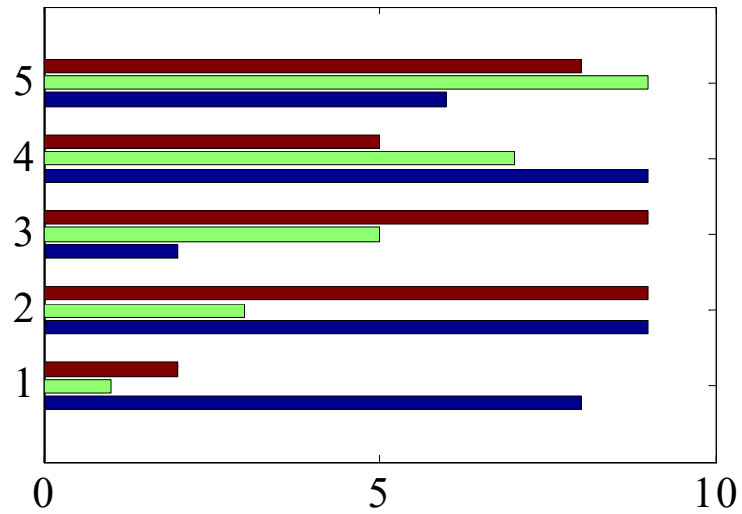
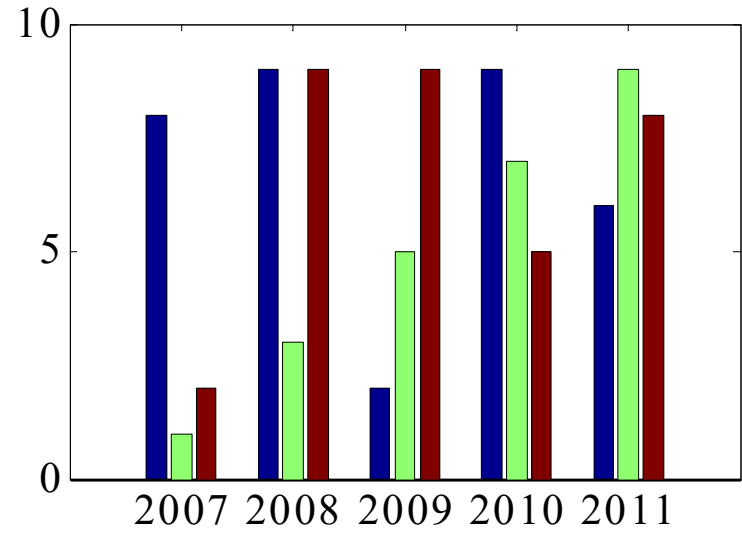
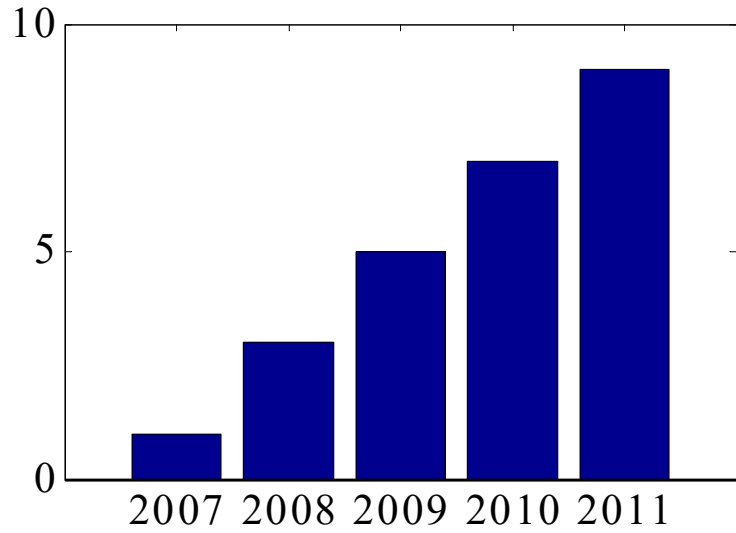
## bar graphs

```
Y = [8 1 2
      9 3 9
      2 5 9
      9 7 5
      6 9 8];

x = 2007:2011; y = Y(:,2);

subplot(2,2,1); bar(x,y);
subplot(2,2,2); bar(x,Y);
subplot(2,2,3); barh(Y);
subplot(2,2,4); bar(Y);
```

# bar graphs



# histograms

initialize generator

```
rng(101);  
b = 0:5:100;  
g = ceil(70 + 12 * randn(1,600));
```

define bins

simulate 600  
random grades

```
figure; H = hist(g,b);
```

H = vector of histogram values

```
xaxis(0,105, 0:10:100);  
title('grade distribution');
```

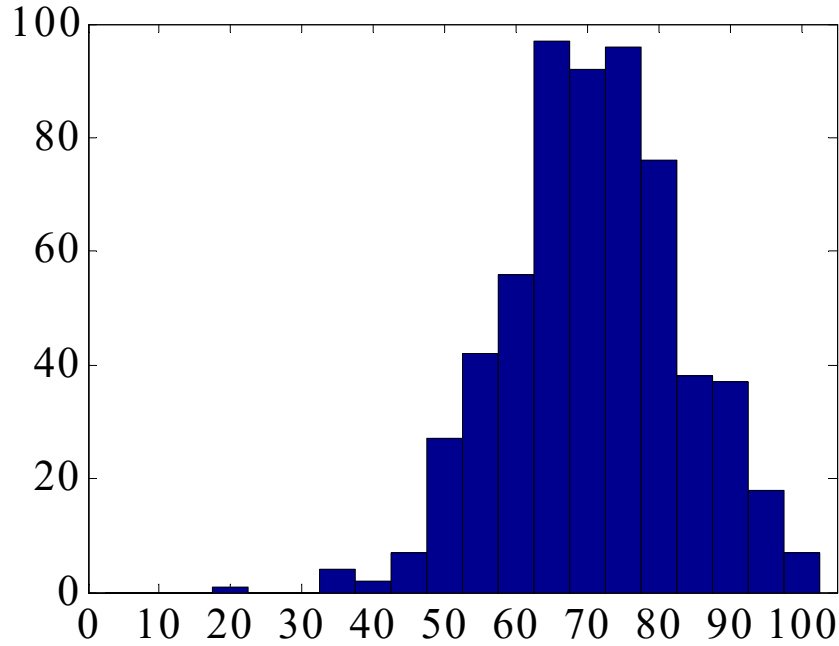
```
figure; H = hist(g,b);
```

improved version

```
h = findobj(gca, 'Type', 'patch');  
set(h, 'FaceColor', 'b', 'EdgeColor', 'w');  
  
xaxis(0,105,0:10:100);  
title('grade distribution');  
line([0,105],[0,0], 'linewidth', 0.3);
```

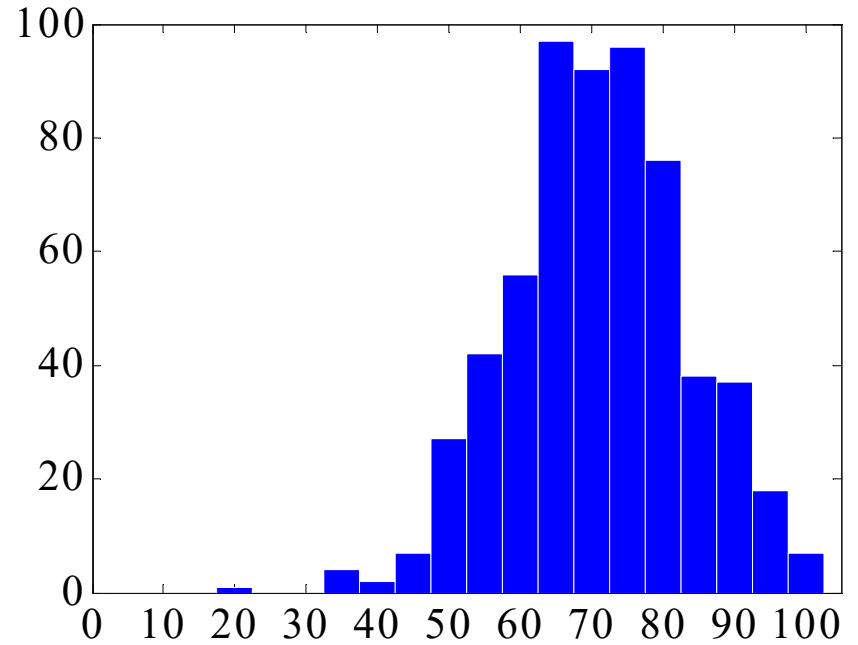
# histograms

grade distribution



← default

grade distribution



improved →

mean = 70.86  
std = 12.39  
median = 71  
mode = 69



pie charts

```

Na = length(find(g>=90));
Nbp = length(find(g<90 & g>=85));
Nb = length(find(g<85 & g>=75));
Ncp = length(find(g<75 & g>=70));
Nc = length(find(g<70 & g>=60));
Nd = length(find(g<60 & g>=50));
Nf = length(find(g<50));
N = [Nf, Nd, Nc, Ncp, Nb, Nbp, Na];
pie(N, {'F', 'D', 'C', 'C+', 'B', 'B+', 'A'});
colormap cool;

```

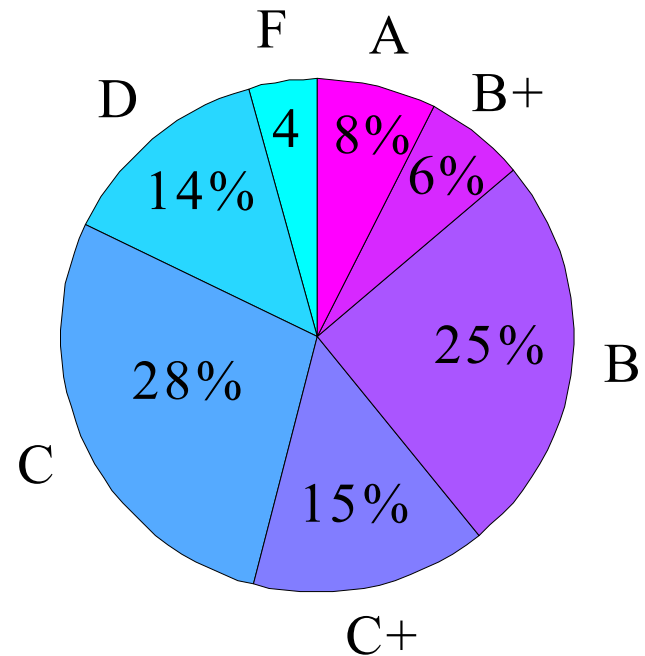
number of A's, B+'s, B's, etc.

```

Nper = round(100 * N/sum(N))

```

percentages were added using the plot editor

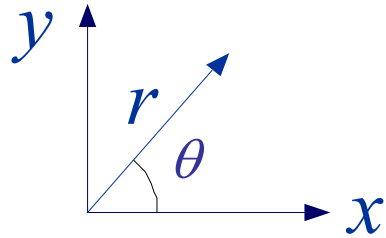


```

% N = [26 81 169 89 152 38 45];
      F D C C+ B B+ A

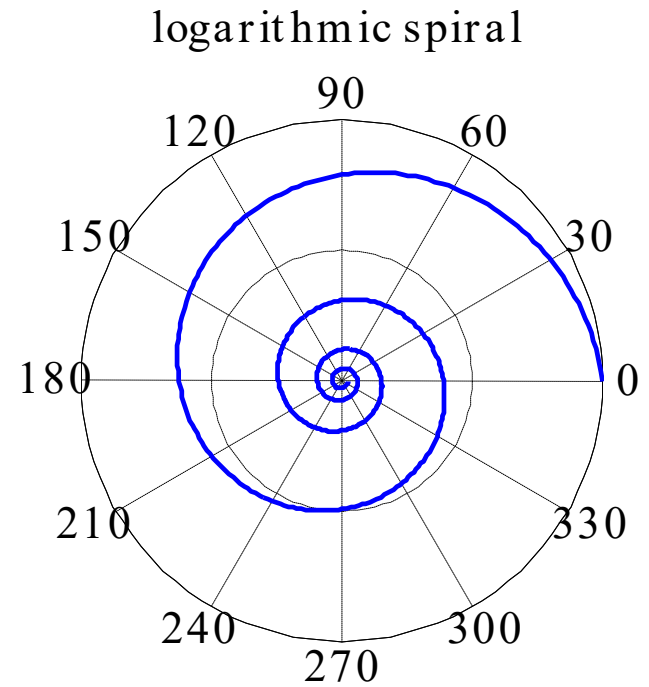
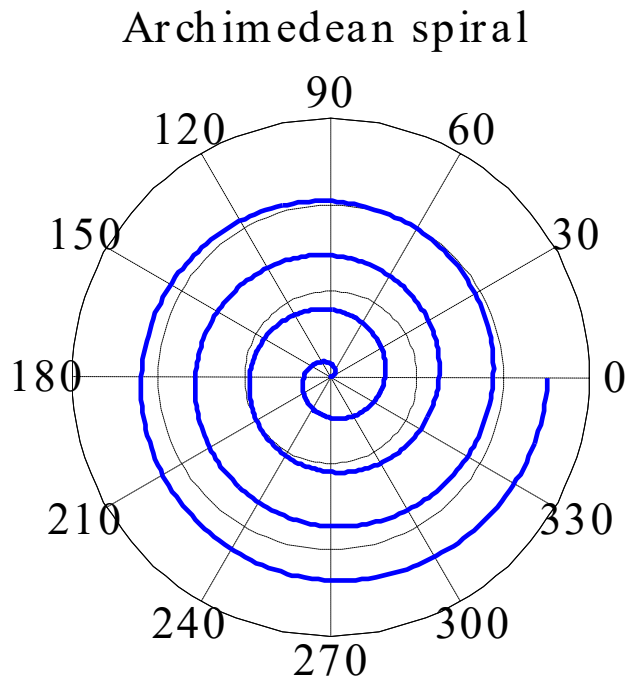
```

polar functions  
 $r = f(\theta)$



polar plots

```
th = linspace(0,8*pi,800);  
r = th;  
polar(th,r);
```



```
r = exp(-0.15*th);  
polar(th,r);
```

## 3D plotting functions

<code>plot3,ezplot3</code>	x-y-z line plot
<code>contour,ezcontour</code>	contour plot
<code>contourf,ezcontourf</code>	filled contour plot
<code>mesh,ezmesh</code>	wireframe surface plot
<code>meshc,ezmeshc</code>	wireframe plus contour
<code>meshz</code>	wireframe with curtain
<code>surf,ezsurf</code>	solid surface plot
<code>surfc,ezsurfc</code>	surface plot plus contour
<code>waterfall</code>	waterfall plot
<code>stem3,scatter3</code>	3D stem and scatter
<code>bar3,bar3h,pie3</code>	3D bar & pie charts
<code>fill3</code>	polygon fill
<code>comet3</code>	animated <code>plot3</code>

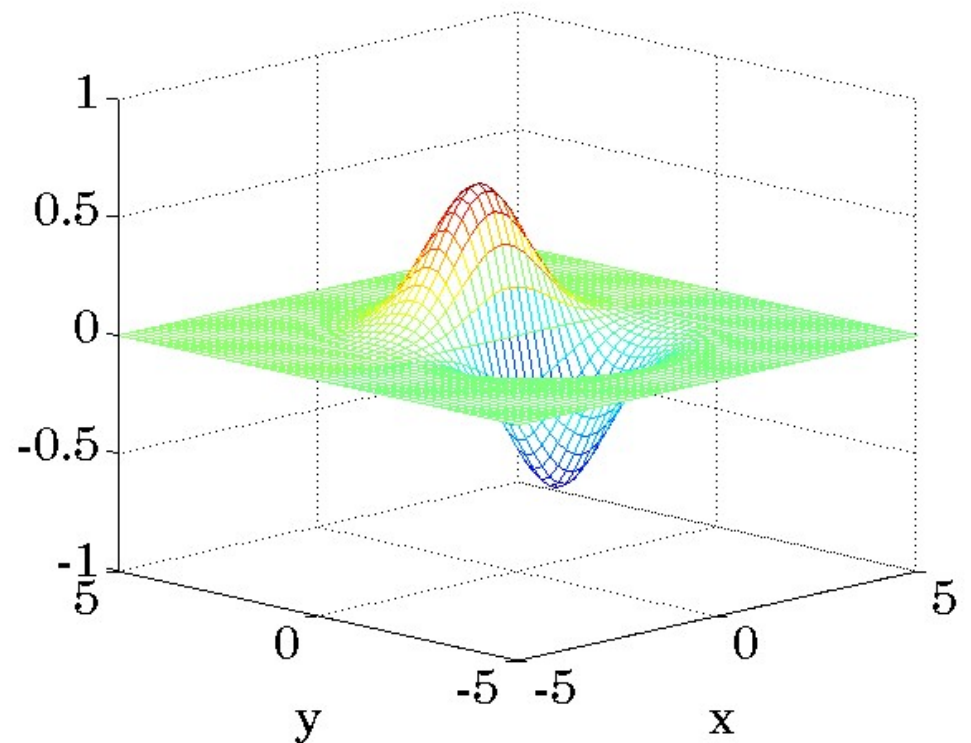
**meshgrid**

was discussed in week-3

```
x = linspace(-5,5,51);  
y = linspace(-5,5,51);  
  
[X,Y] = meshgrid(x,y);  
  
Z = Y .* exp(-(X.^2 + Y.^2)/2);  
  
mesh(X,Y,Z);
```

mesh

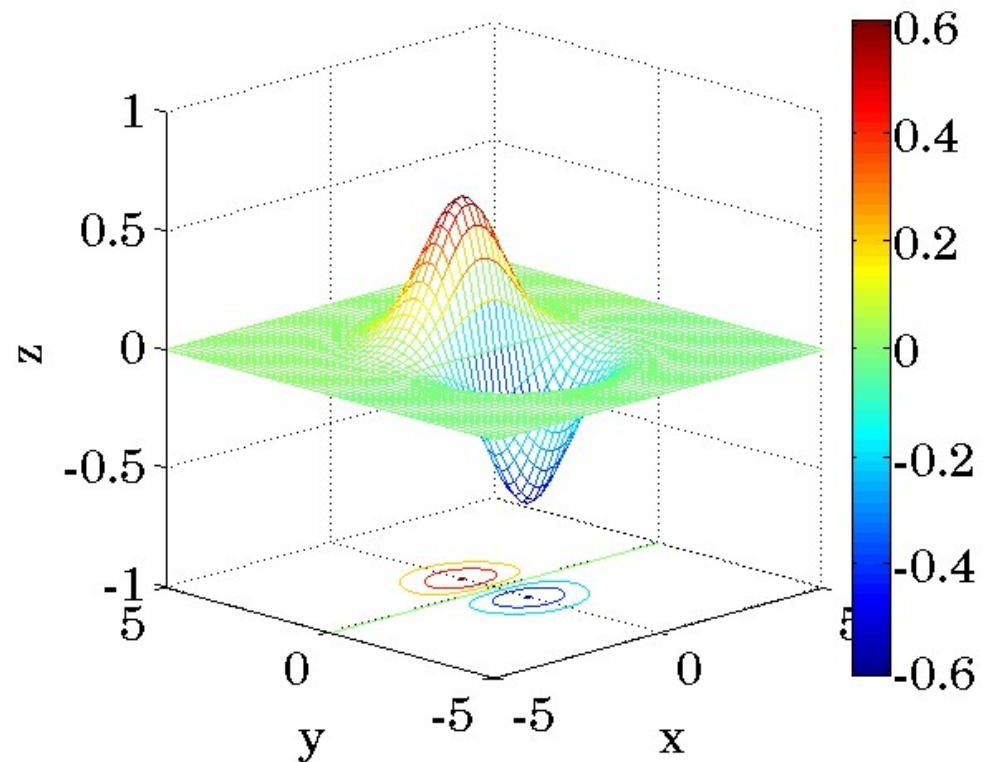
$$z = f(x, y) = y \exp(-(x^2 + y^2)/2)$$



```
meshc(X,Y,Z);  
view(-45,15);  
colorbar;
```

meshc

```
>> doc view;  
>> doc colorbar;  
>> doc colormap;
```



contour  
contourf

number of contour levels

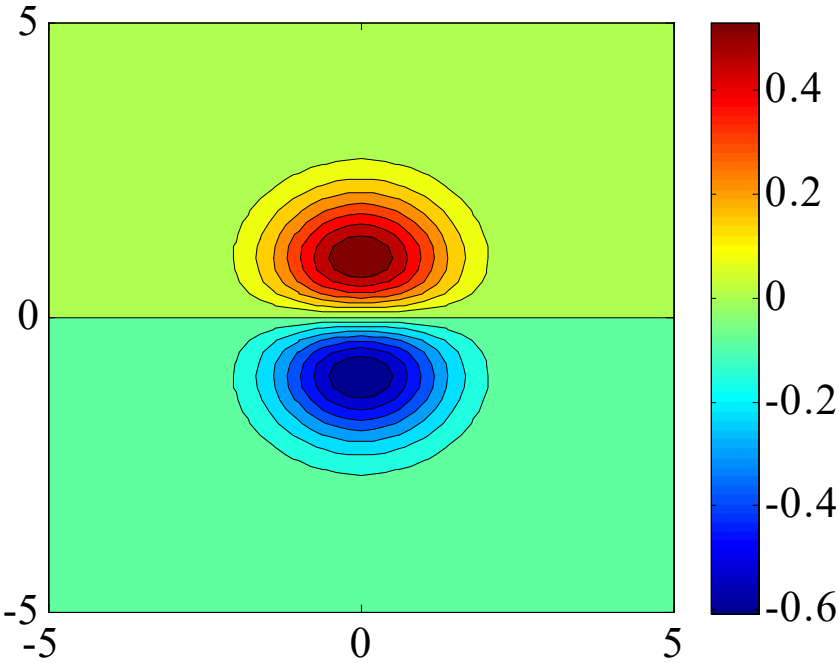
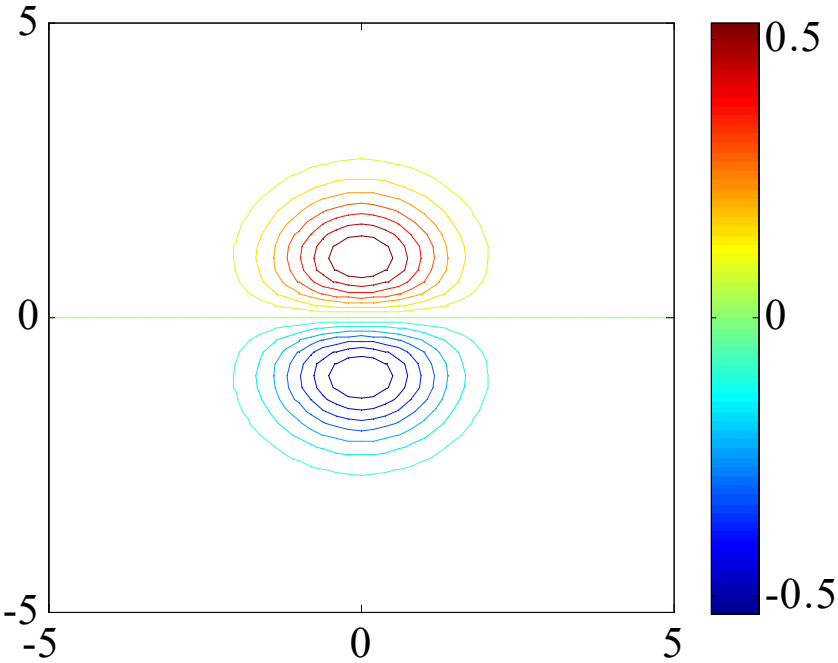


```
contour(X,Y,Z,15);  
colorbar;
```

filled contour



```
contourf(X,Y,Z,15);  
colorbar;
```

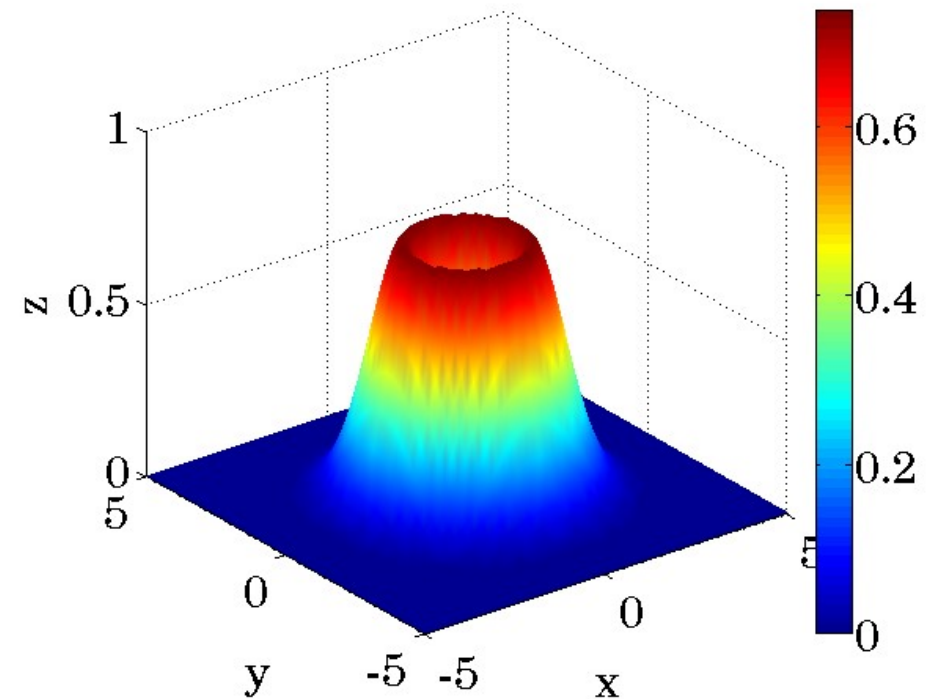
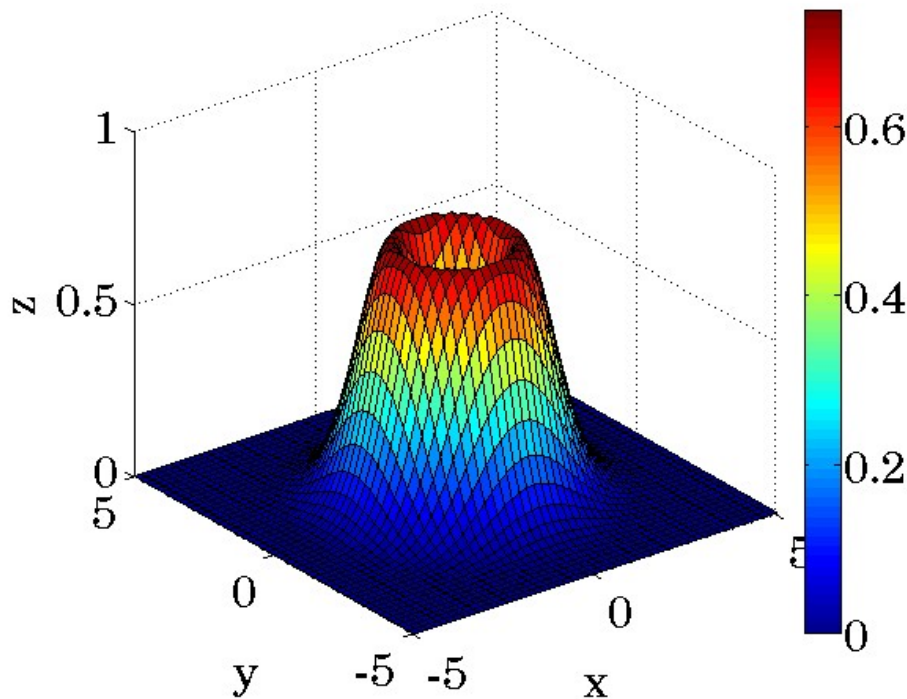


```
x = linspace(-5,5,51);  
y = linspace(-5,5,51);  
[X,Y] = meshgrid(x,y);  
Z = (X.^2 + Y.^2) .* exp(-(X.^2 + Y.^2)/2);
```

surf

```
surf(X,Y,Z);  
colorbar;
```

```
surf(X,Y,Z);  
shading interp;  
colorbar;
```

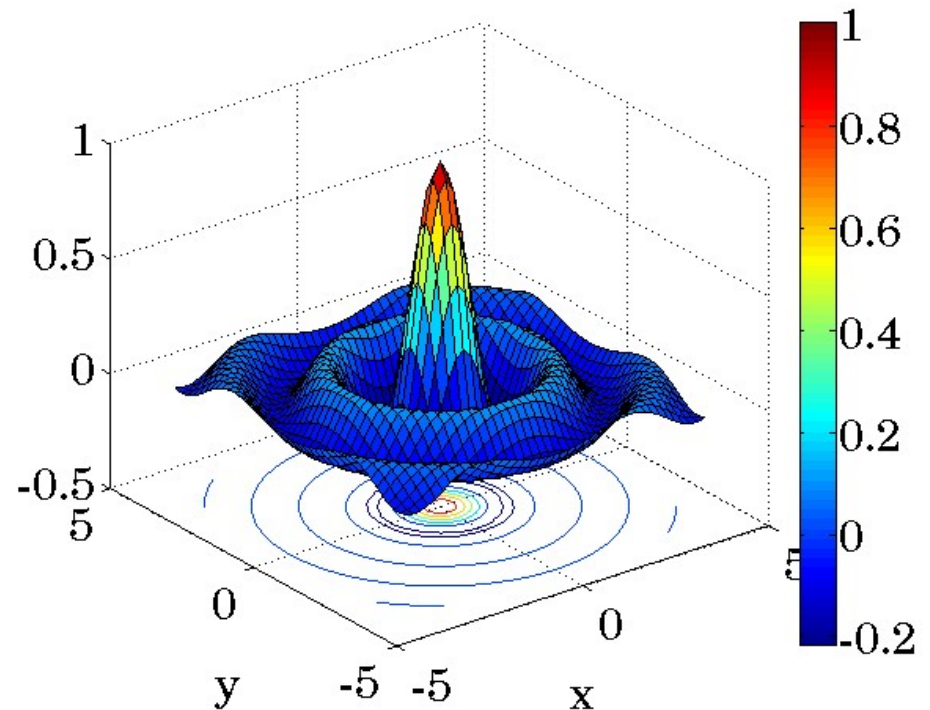
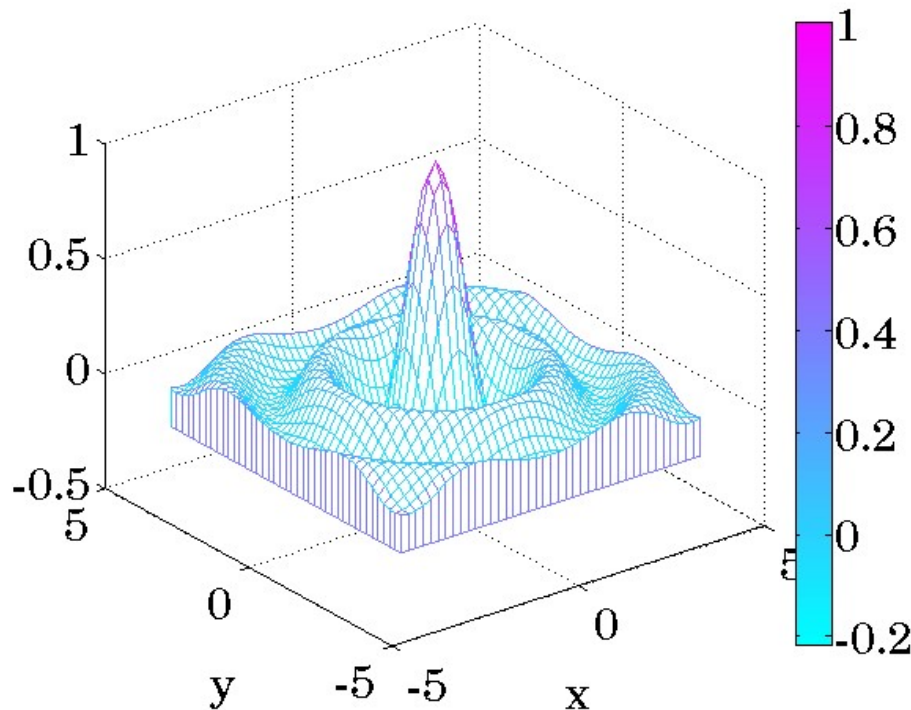


```
x = linspace(-4,4,41);  
y = linspace(-4,4,41);  
[X,Y] = meshgrid(x,y);  
Z = sinc(sqrt(X.^2 + Y.^2)); % help sinc
```

meshz  
surf

```
meshz(X,Y,Z);  
colormap cool;  
colorbar;
```

```
surf(X,Y,Z);  
colorbar;
```





surf

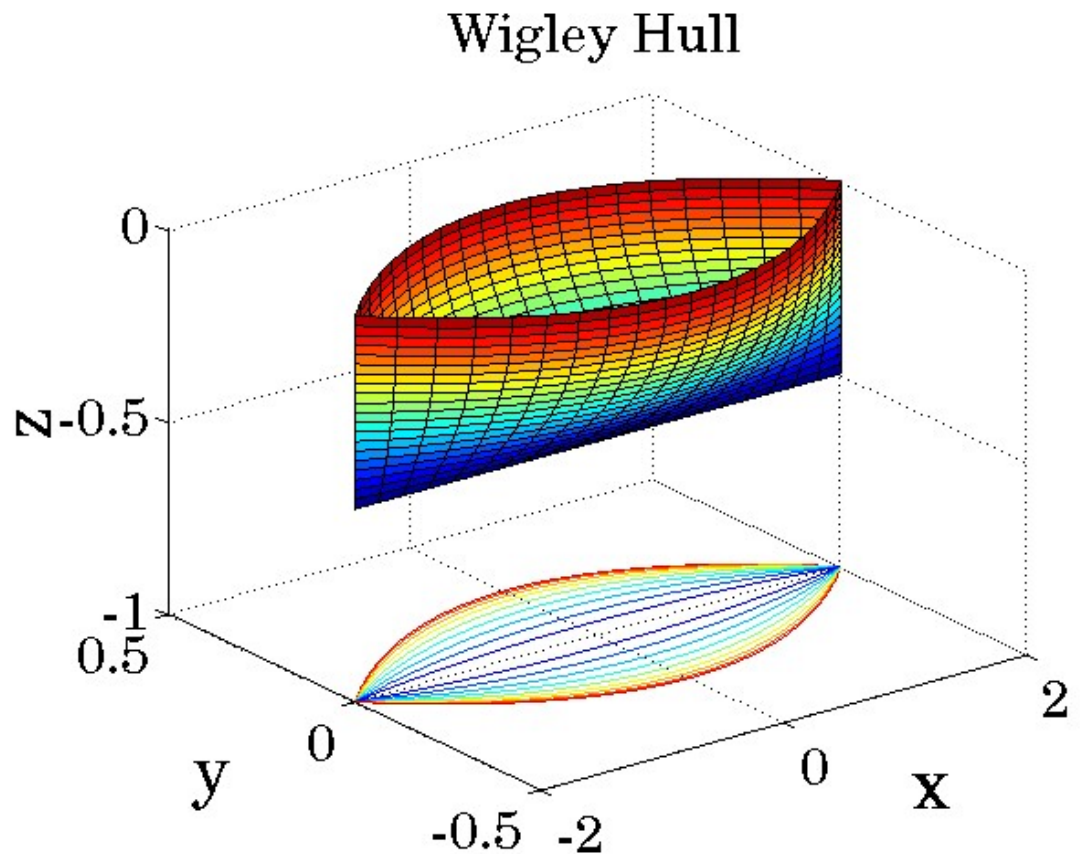
```
B = 0.5; L = 4; D = 0.5;  
x = linspace(-L/2, L/2, 21);  
z = linspace(-D, 0, 21);  
[X,Z] = meshgrid(x,z);  
  
Y = B/2 * (1 - 4*X.^2/L^2) .* (1 - Z.^2/D.^2);  
  
figure;  
surf(X,Y,Z);  
hold on;  
surf(X,-Y,Z);
```

Wigley Hull

$$y = \pm \frac{B}{2} \left(1 - \frac{4x^2}{L^2}\right) \left(1 - \frac{z^2}{D^2}\right)$$

Reference:

A. Gilat, MATLAB, An Introduction with Applications, 4/e, Wiley, 2011



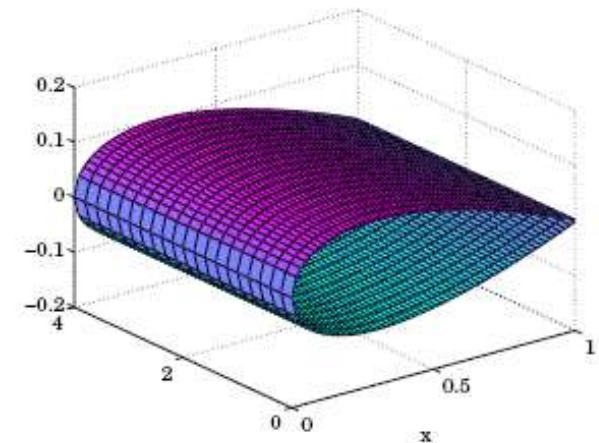
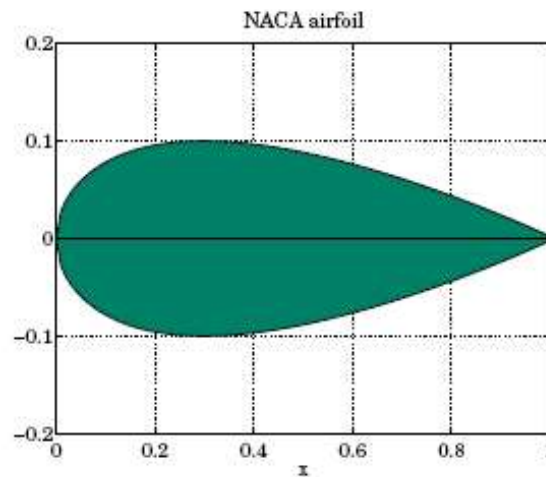
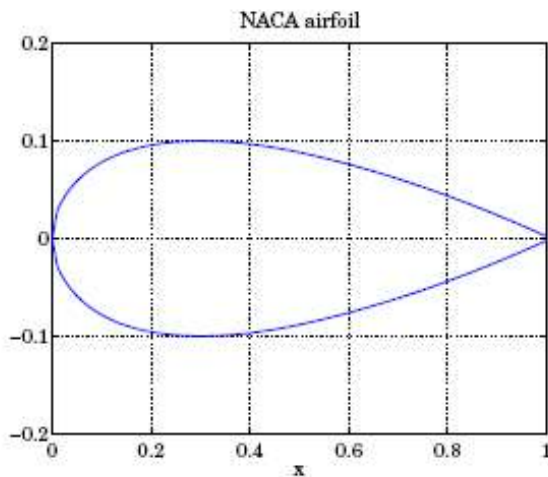
National Advisory Committee for Aeronautics

NACA airfoils

area

$$y = \pm \frac{tc}{0.2} \left[ 0.2969 \sqrt{\frac{x}{c}} - 0.1260 \left(\frac{x}{c}\right) - 0.3516 \left(\frac{x}{c}\right)^2 + 0.2843 \left(\frac{x}{c}\right)^3 - 0.1015 \left(\frac{x}{c}\right)^4 \right]$$

$$0 \leq x \leq c$$



Reference:

A. Gilat, MATLAB, An Introduction with Applications, 4/e, Wiley, 2011

```
c = 1; t = 0.2;

f = @(x) t*c/0.2 * (0.2969*sqrt(x/c) ...
    - 0.1260*(x/c) - 0.3516*(x/c).^2 ...
    + 0.2843*(x/c).^3 - 0.1015*(x/c).^4);

x = linspace(0,c,101);

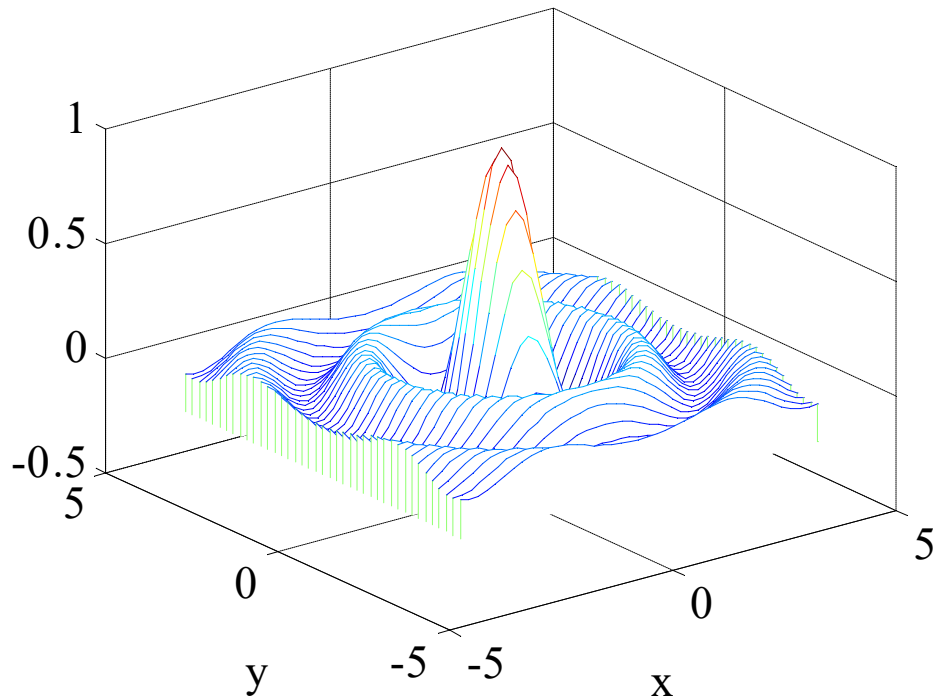
y = f(x);

figure; plot(x,y,'b-', x,-y,'b-');
figure; area(x,y); hold on; area(x,-y);
colormap summer;

w = 4;
y = 0:w/20:w;
x = 0:c/60:c;

[X,Y] = meshgrid(x,y);
Z = f(X);

figure; surf(X,Y,Z); hold on; surf(X,Y,-Z);
colormap cool;
```



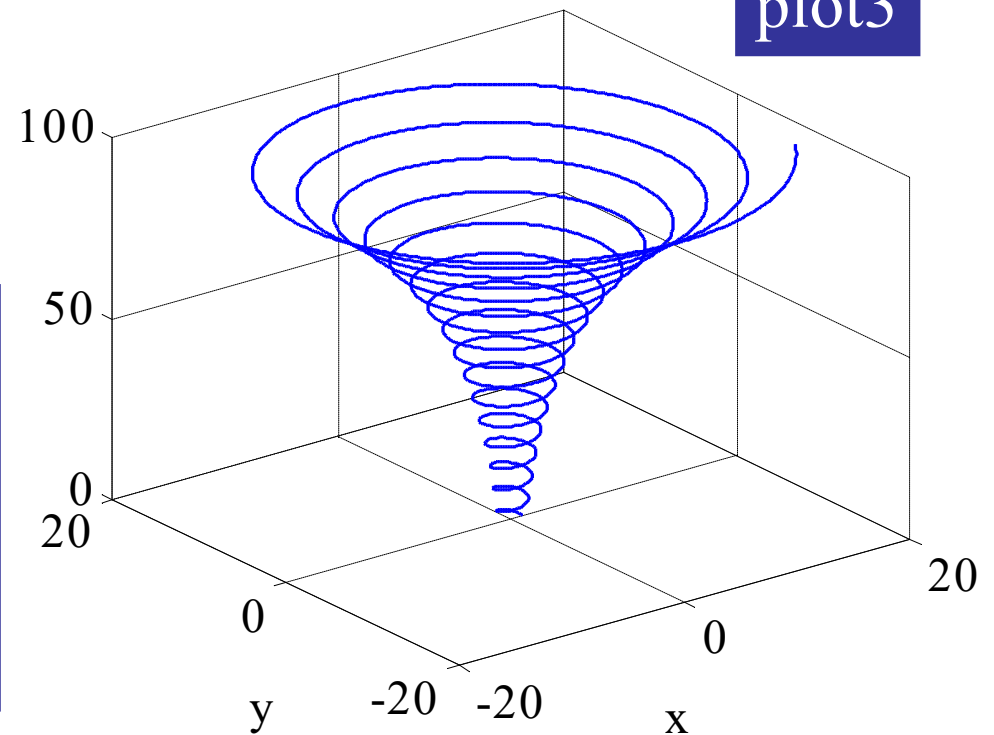
waterfall

unidirectional  
mesh plot

`waterfall(X,Y,Z);`

```
t = 0:0.01:100;
x = exp(0.03*t).*cos(t);
y = exp(0.03*t).*sin(t);
z = t;
plot3(x,y,z,'b');
grid on;
```

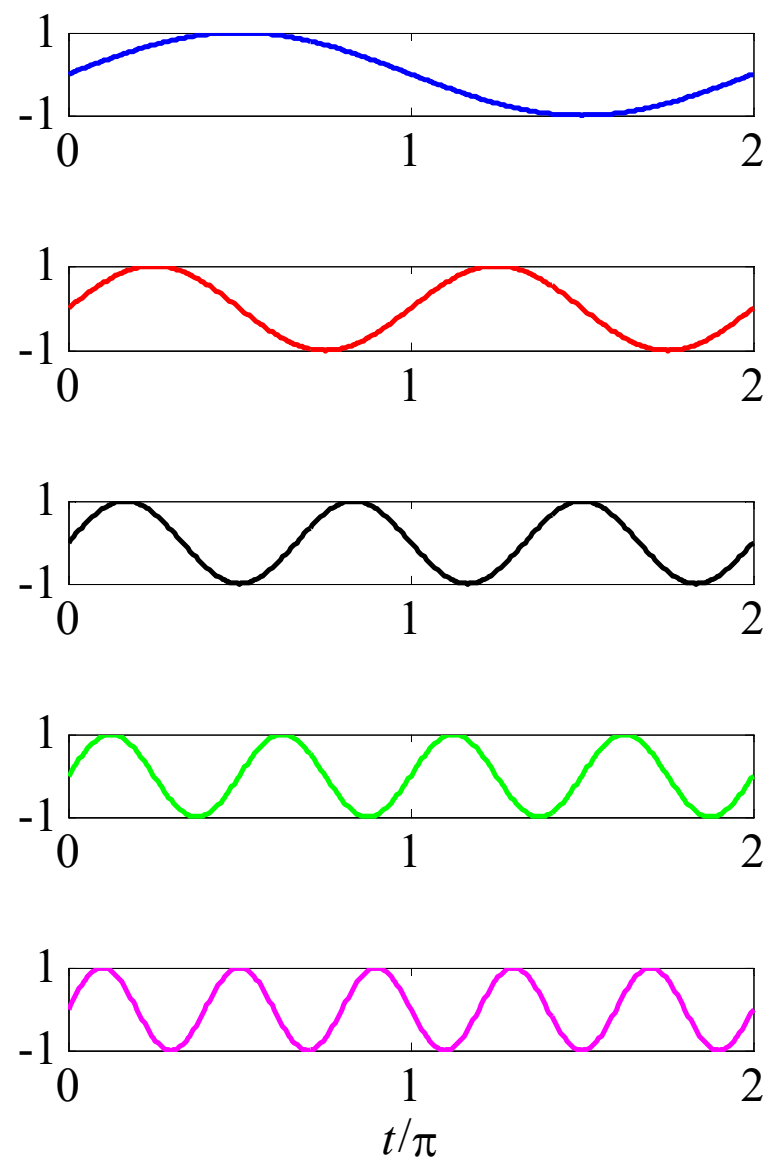
plot3



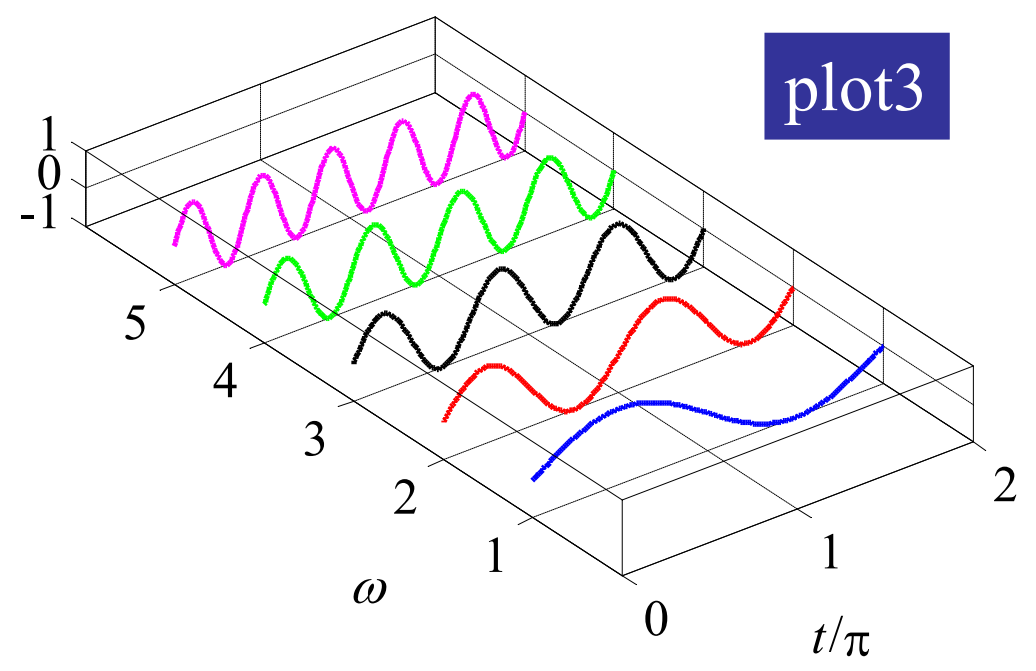
How to display  
multiple curves  
three-dimensionally

e.g.,  $\sin(\omega t)$ ,  
for  $\omega = 1, 2, 3, 4, 5$

subplot



plot3



```
t = linspace(0,2*pi,361);  
  
C = {'b', 'r', 'k', 'g', 'm'};  
  
for k=1:5,  
    subplot(5,1,k);  
    z = sin(k*t);  
    plot(t/pi,z,'color',C{k});  
    xaxis(0,2, 0:2);  
    yaxis(-1,1, [-1,1]);  
end  
  
xlabel('t/\pi');
```

subplot

```
t = linspace(0,2*pi,361);
y1 = ones(size(t));

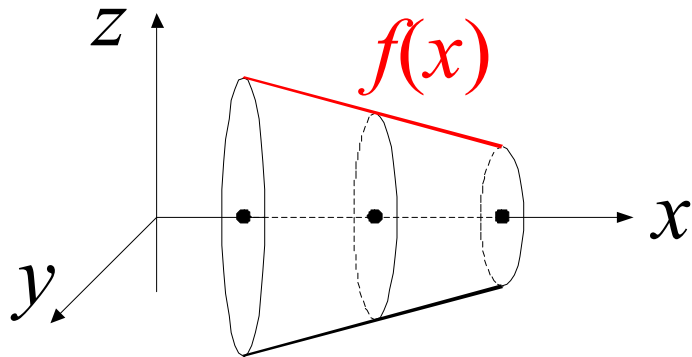
C = {'b', 'r', 'k', 'g', 'm'};

for k=1:5,
    z = sin(k*t);
    plot3(t/pi, k*y1, z, 'color',C{k});
    hold on;
end

hold off; box on; grid on;
xaxis(0,2, 0:2); yaxis(0,6, 1:5);
xlabel('t/\pi'); ylabel('\omega');

set(gca, 'DataAspectRatio', [1, 1.5, 5]);
```

plot3



How to generate surfaces of revolution, e.g., rotating a function  $z = f(x)$  about the  $x$ -axis

```
x = linspace(a,b,N);
theta = linspace(0,2*pi,M);

[X,Th] = meshgrid(x,theta);

Y = f(X) .* cos(Th);
Z = f(X) .* sin(Th);

surf(X,Y,Z);      % or mesh()
```

assume  $f(x)$  is defined over  $a \leq x \leq b$

to rotate a function  $f(z)$  about the  $z$ -axis, simply interchange roles of  $x, z$ , but do **surf(X,Y,Z)**

or, use the built-in function **cylinder**



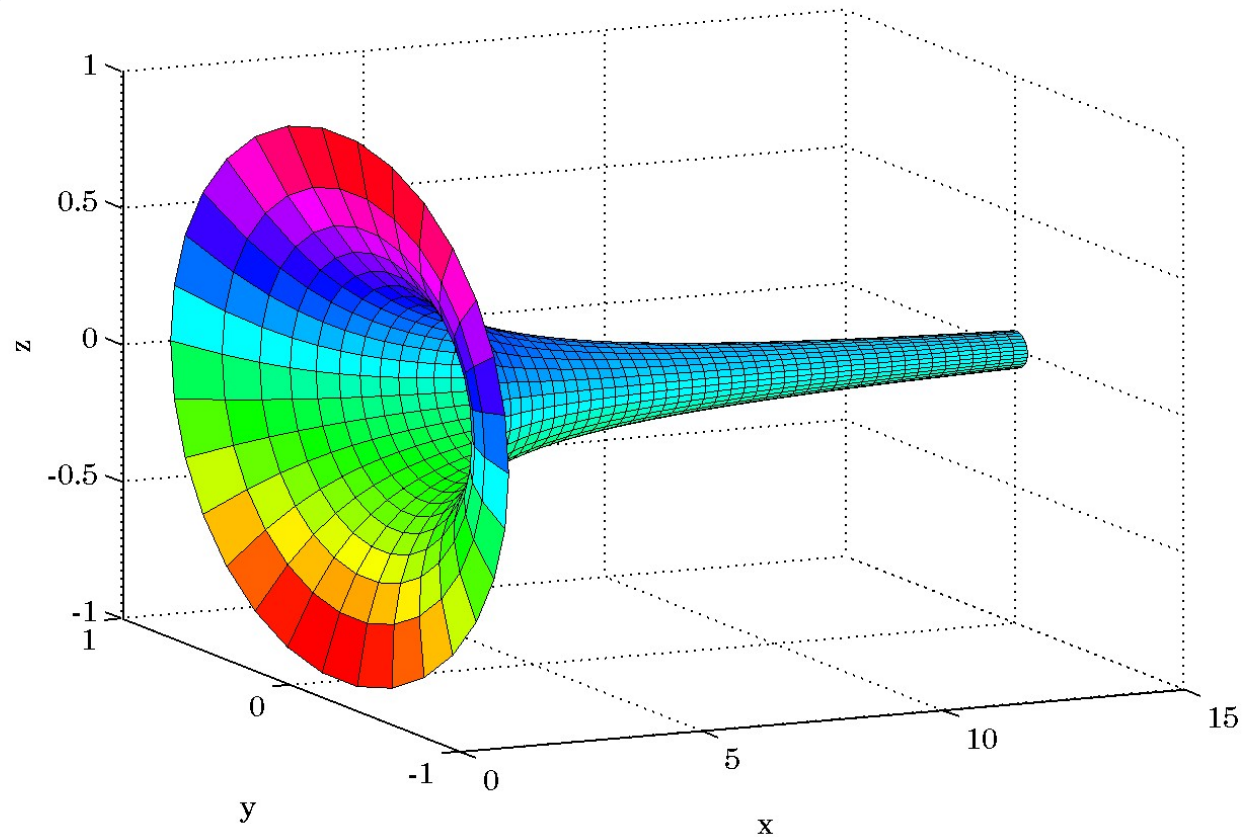
```
x = linspace(1,15,50);  
th = linspace(0,2*pi,31);  
  
[X,Th] = meshgrid(x,th);  
  
F = 1./X;  
Y = F.*cos(Th);  
Z = F.*sin(Th);
```

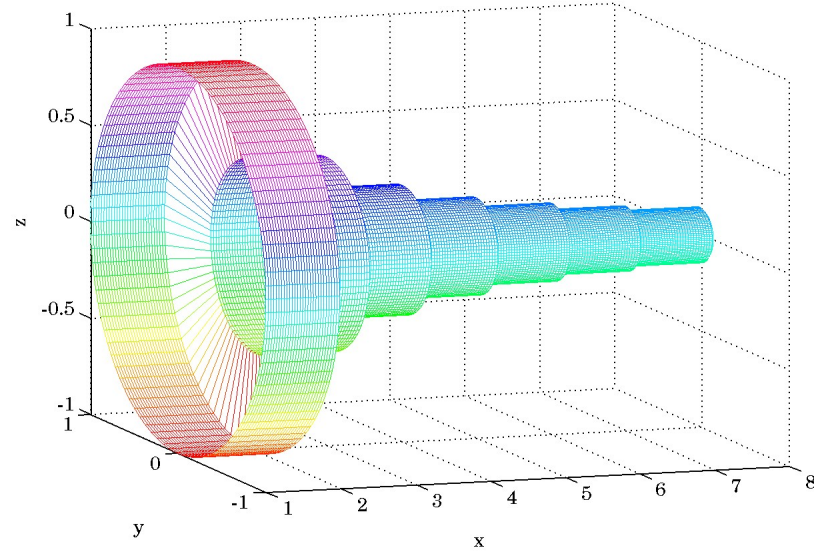
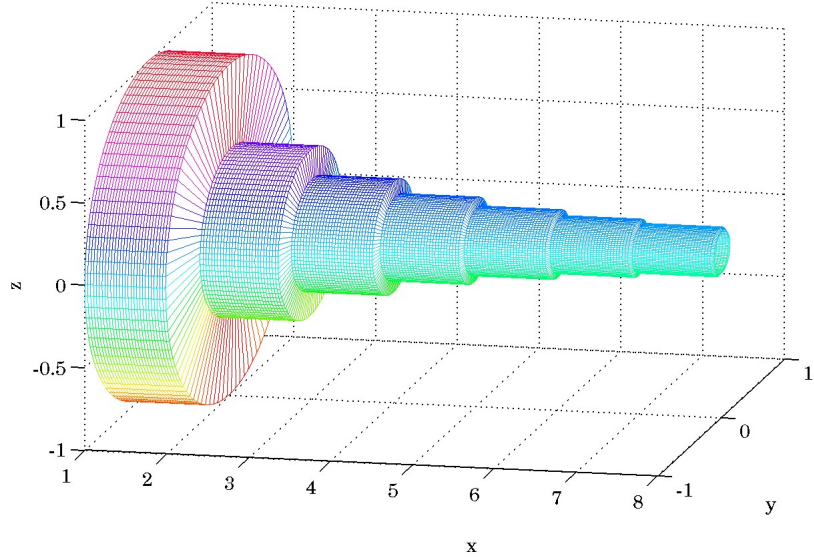
```
surf(X,Y,Z);  
view(-25,15);  
colormap hsv;
```

has finite volume,  
but infinite area

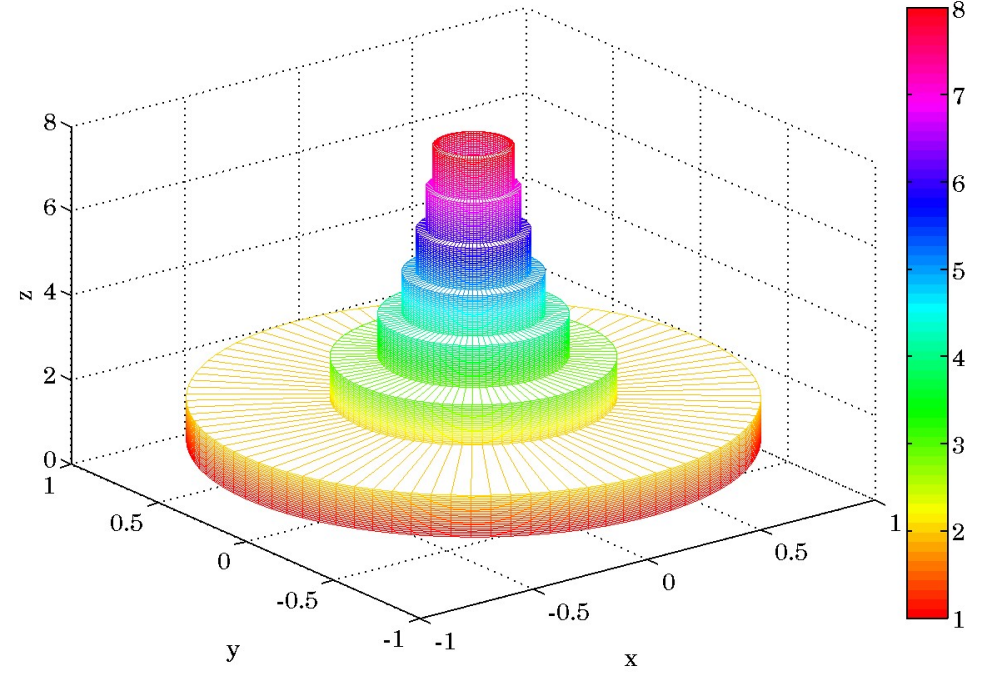
Torricelli's Trumpet,  
aka Gabriel's Horn,

$$f(x) = 1/x, \quad 1 \leq x < \infty$$





Gabriel's Cake  
 uses a step version  
 of  $f(x) = 1/x$



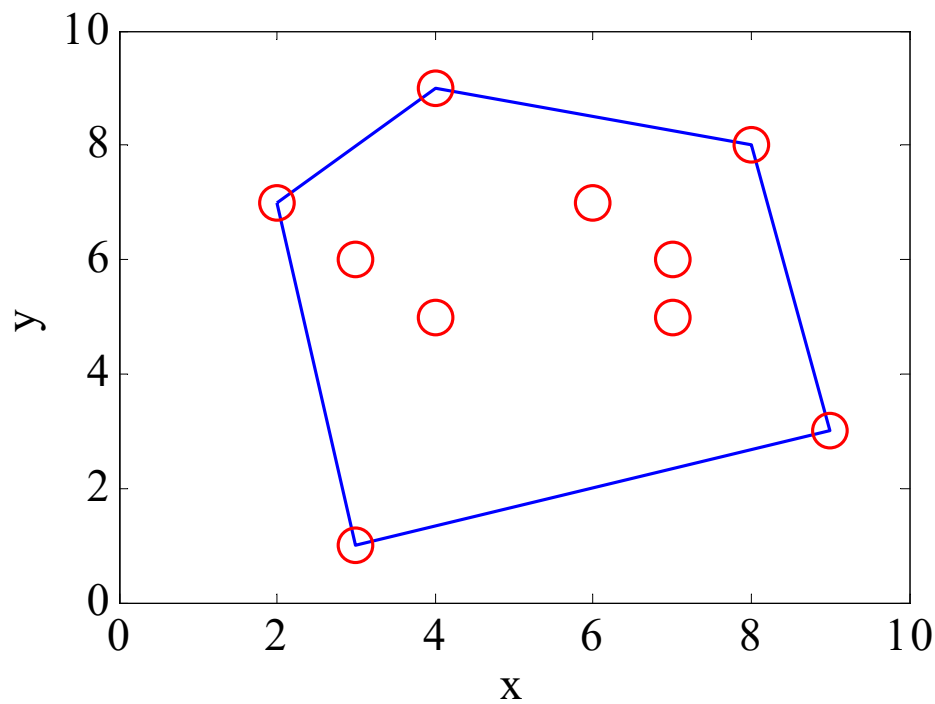
```
x = [6,3,2,7,4,3,9,4,8,7];  
y = [7,6,7,6,5,1,3,9,8,5];
```

```
n = convhull(x,y);  
plot(x(n),y(n),'b-',x,y,'ro');
```

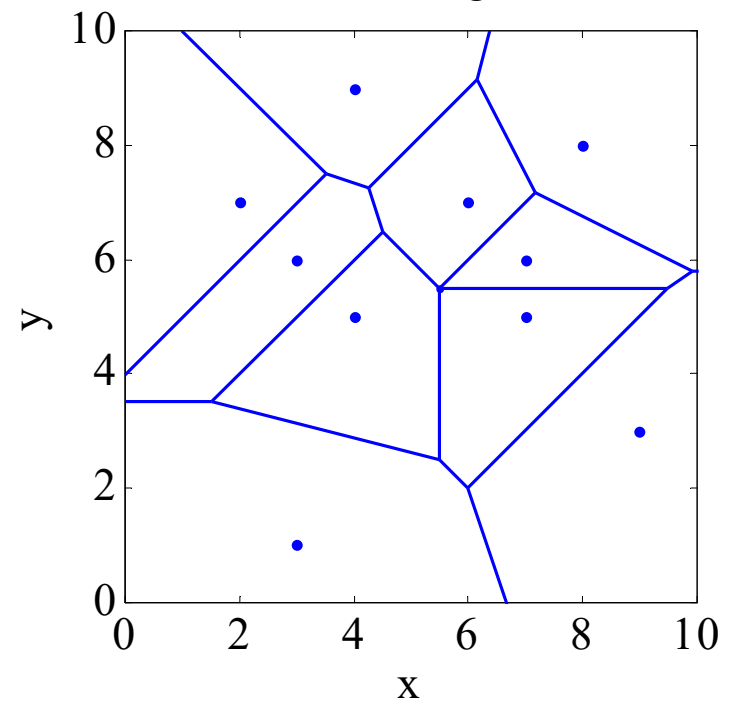
convhull  
voronoi

```
voronoi(x,y,'b-');
```

convex hull



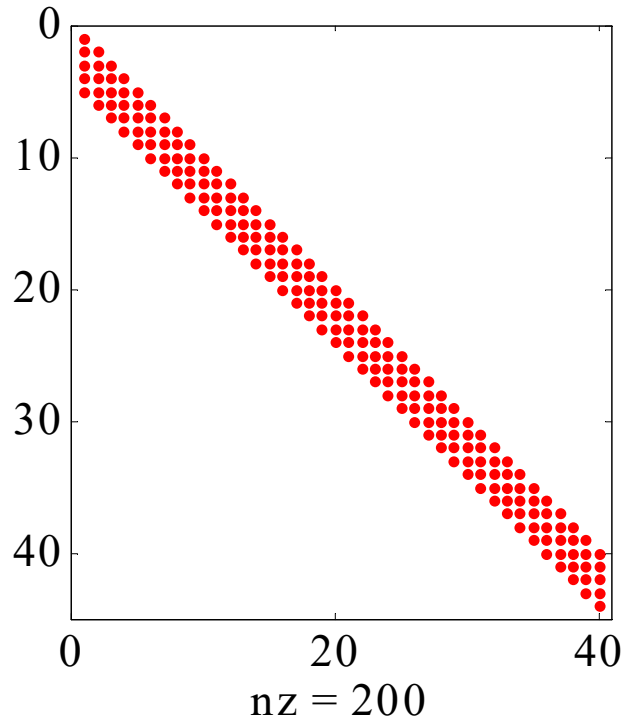
voronoi diagram



spy

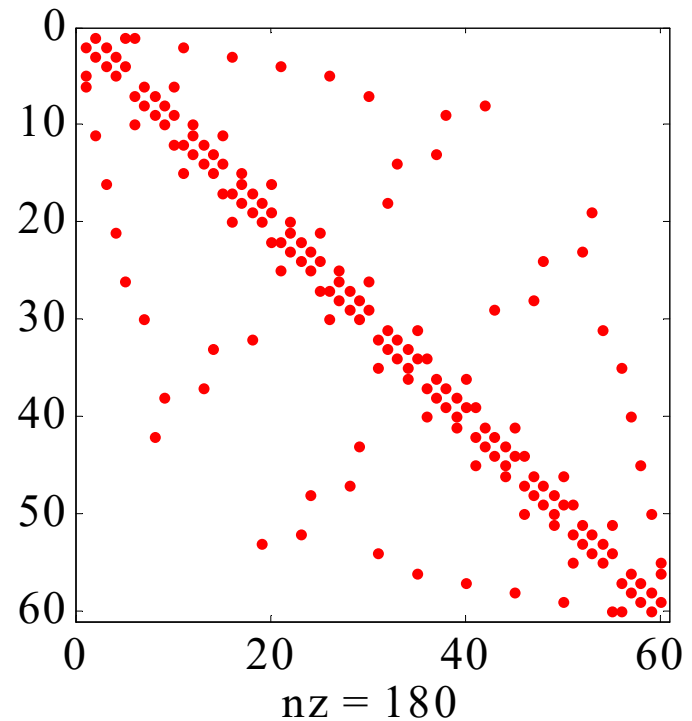
sparsity pattern

```
h = [2 3 5 8 4]';  
N = 40;  
H = convmtx(h,N);  
spy(H,'r.');
```



convolution matrix

```
B = bucky; spy(B,'r.');
```



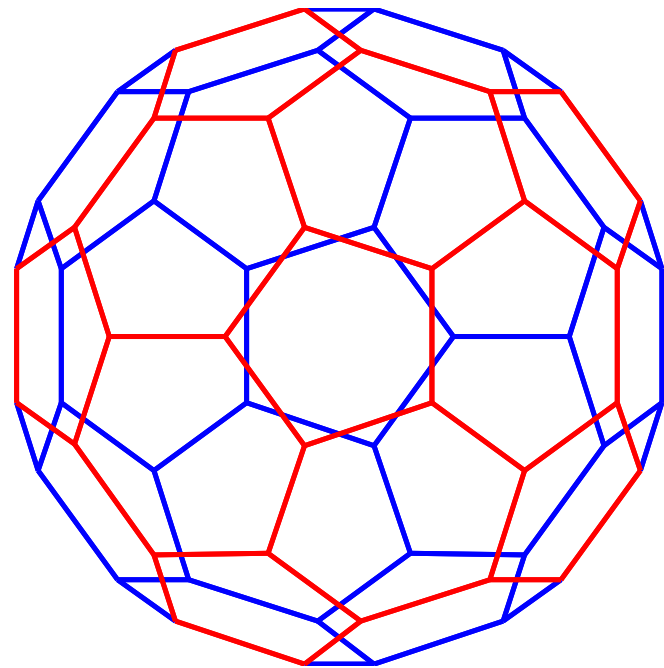
60 x 60 sparse adjacency matrix  
of the connectivity graph of the  
Bucky ball, geodesic dome, soccer ball,  
and the carbon-60 fullerene  
molecule

```
[B,V] = bucky;  
H = sparse(60,60);  
k = 31:60;  
H(k,k) = B(k,k);  
  
% Visualize the variables  
gplot(B-H,V,'b-');  
hold on  
gplot(H,V,'r-');  
axis off equal square
```

MATLAB code from [here](#)

gplot

plotting connectivity,  
or, adjacency matrices

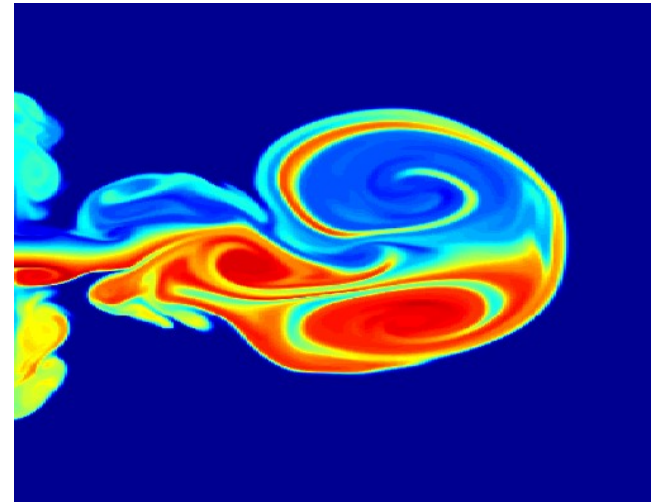


## Examples of loading images

```
load earth;  
image(X);  
colormap(map);  
axis square; axis off
```

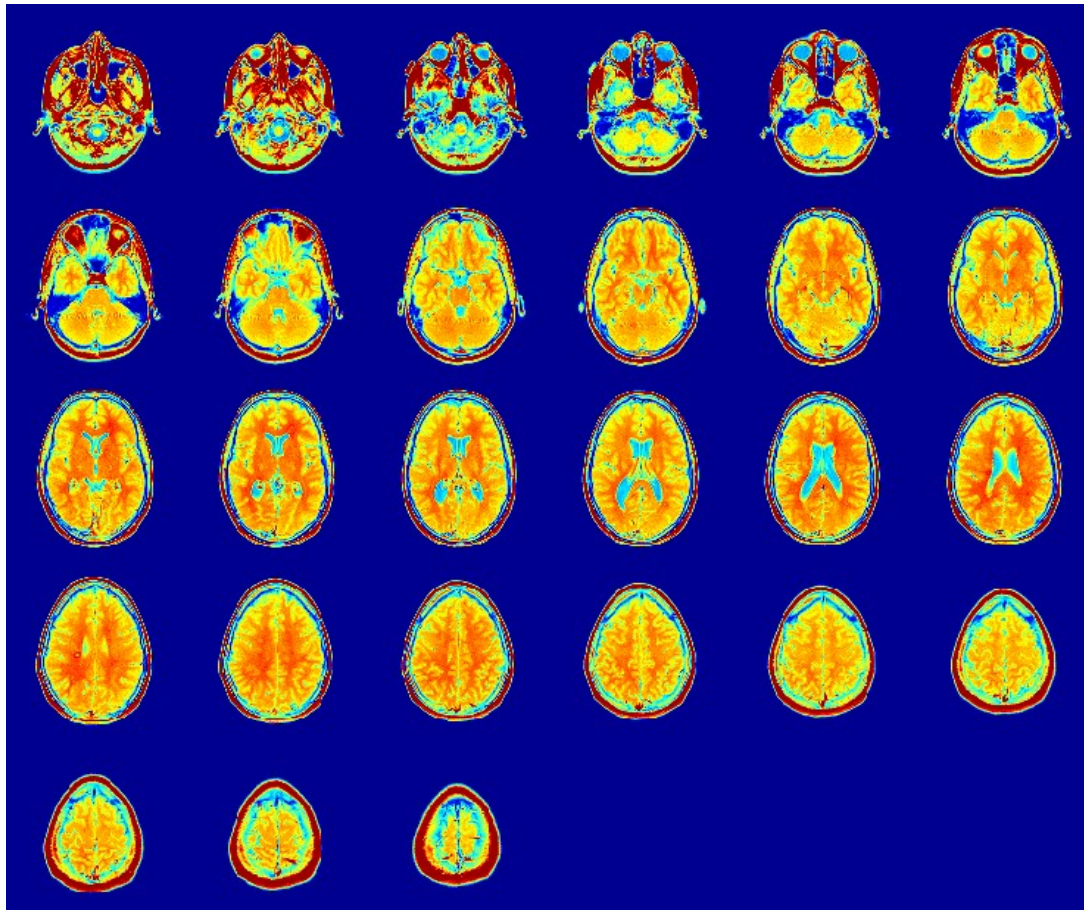


```
load flujet;  
image(X);  
axis off
```



```
load mri;  
montage(D,jet);  
title('Horizontal Slices');
```

Horizontal Slices



## Reading & writing image files

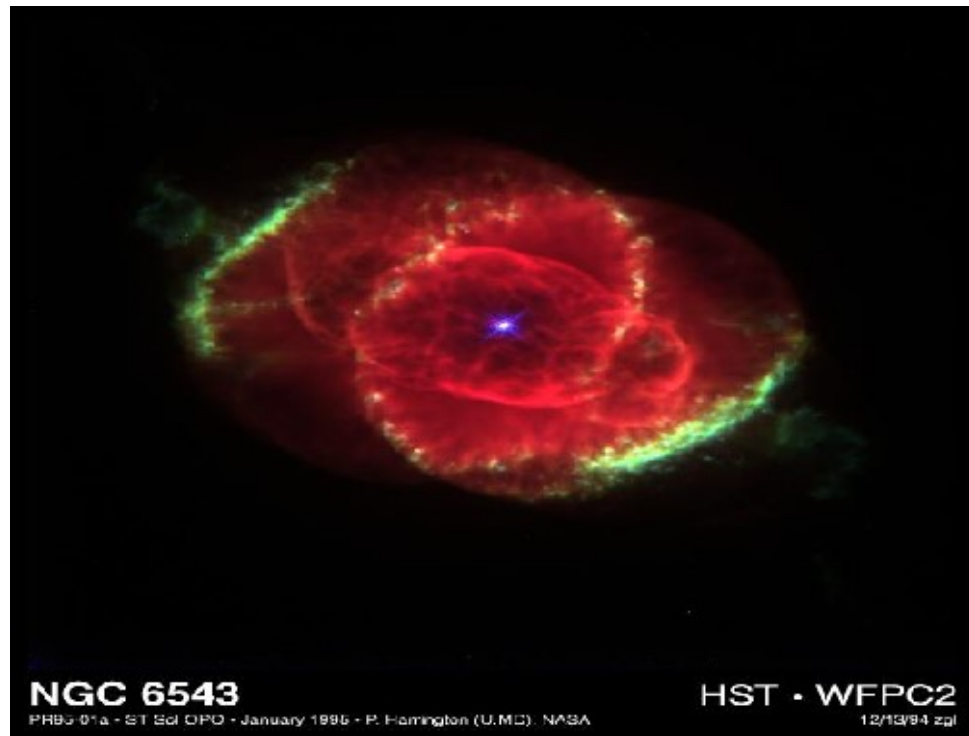
```
A = imread(filename, fmt);  
[A, map] = imread(filename, fmt);  
  
imwrite(A, filename, fmt);  
  
imfinfo(filename);  
  
fmt: 'jpg', 'jp2', 'tiff', 'png',  
      'gif', 'bmp', and others
```

these functions have additional input/output options

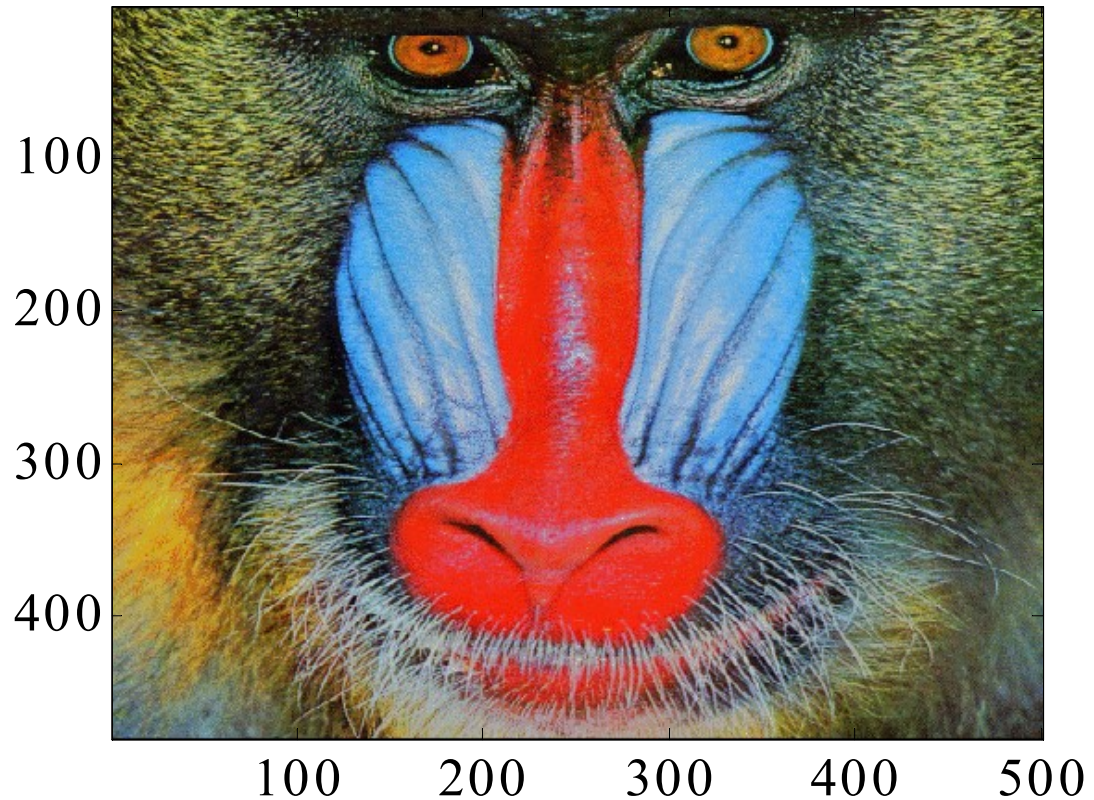


```
y = imread('ngc6543a.jpg', 'jpg');  
image(y);  
title('NGC 6543 Nebula'); axis off;
```

NGC 6543 Nebula



```
load mandrill;           % MATLAB demo image
image(X);                % X,map are part of the
colormap(map);           % saved mandrill.mat file
```



```
s1 = 'http://upload.wikimedia.org/';  
s2 = 'wikipedia/commons/d/de/';  
s3 = 'St_Louis_night_expblend.jpg';  
filename = [s1,s2,s3];
```

```
y = imread(filename, 'jpg');  
image(y); axis off;
```



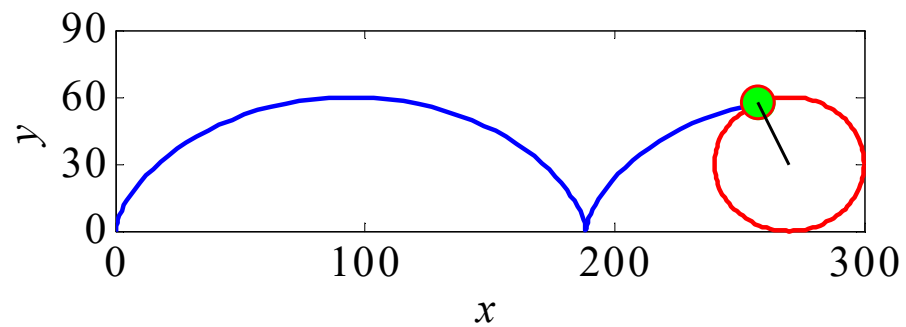
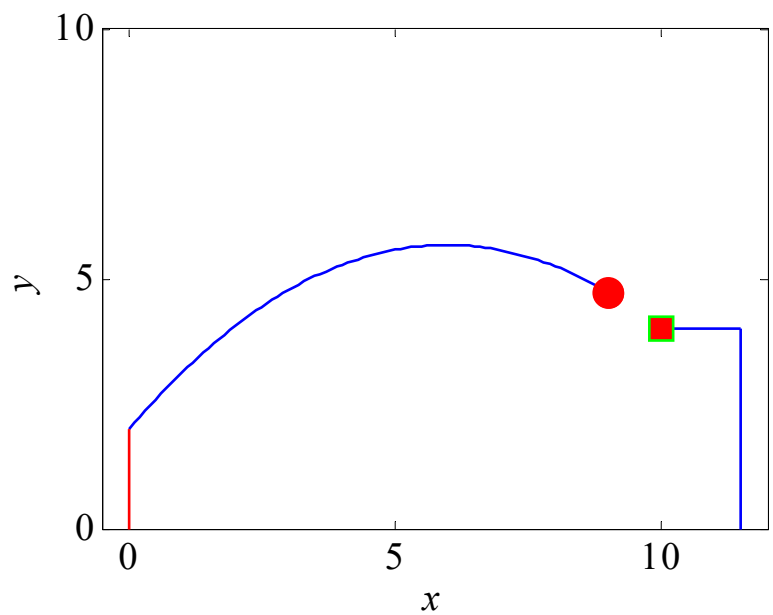
```
'http://upload.wikimedia.org/wikipedia/commons/d/de/St_Louis_night_expblend.jpg'
```

## Finally, movies...

Animated plots can be made with the functions **drawnow**, **getframe**, **movie**

Please study and run the following M-files included in **movies.zip** (placed on sakai) :

- hoops.m** – throwing the perfect basketball shot
- receiver.m** – moving wide-receiver catching a ball thrown by the QB
- cycloid.m** – cycloid curve traced by a point on a rolling wheel
- dipmovie.m** – EM wave emitted by a dipole antenna, e.g., your cell phone (see [Ref. ch.14](#))



$$v = \omega R$$

$$x(t) = R \cos(\omega t)$$

$$y(t) = R \sin(\omega t)$$

